

## Assigning to a Variable

What is the result of this program?

```
let f = proc(x) set x = 1
in let y = 0
in { (f y);
y }
```

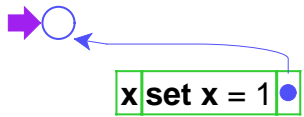
Is it 0 or 1?

## Assigning to a Variable



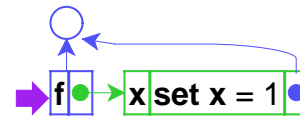
```
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```

## Assigning to a Variable



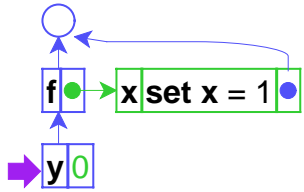
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in { (f y);
y }
```

## Assigning to a Variable



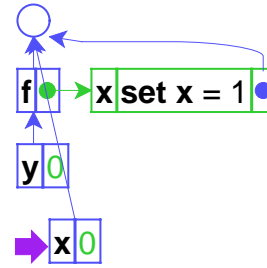
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y }
```

### Assigning to a Variable



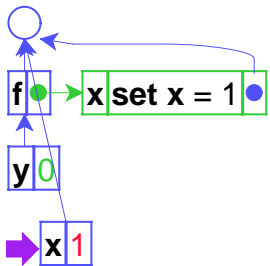
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```

### Assigning to a Variable



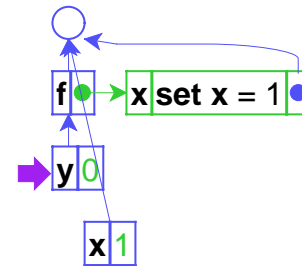
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### Assigning to a Variable



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```

### Assigning to a Variable



```
let f = proc(x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

So the answer is 0

## Variables in C++

```
void f(int x) {
    x = 1;
}

int main() {
    int y = 0;
    f(y);
    return y;
}
```

The result above is 0, too

## Variables in C++

```
void f(int& x) {
    x = 1;
}

int main() {
    int y = 0;
    f(y);
    return y;
}
```

But the result above is 1

## Variables in C++

```
void f(int& x) {
    x = 1;
}

int main() {
    int y = 0;
    f(y);
    return y;
}
```

This example shows *call-by-reference*.

The previous example showed *call-by-value*.

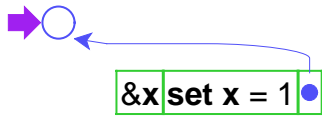
## Assignment and Call-by-Reference



```
let f = proc(&x) set x = 1
in let y = 0
in { (f y);
    y
}
```

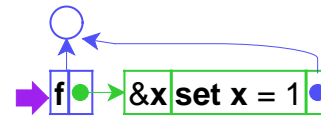
Adding call-by-reference parameters to our language

### Assignment and Call-by-Reference



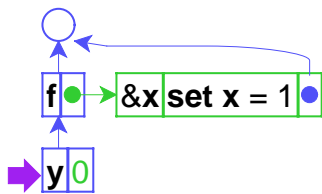
```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

### Assignment and Call-by-Reference



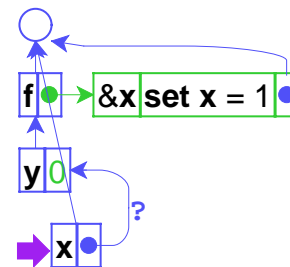
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### Assignment and Call-by-Reference



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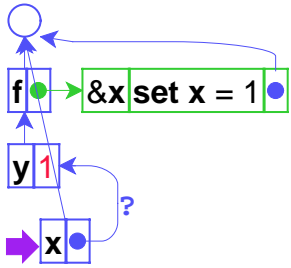
### Assignment and Call-by-Reference



```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

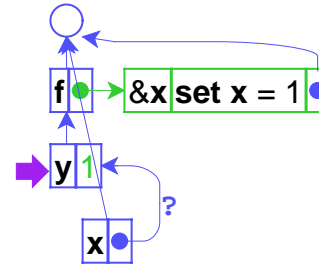
The pointer from one environment frame to another is questionable, because frames are supposed to point to values

## Assignment and Call-by-Reference



```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

## Assignment and Call-by-Reference



```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

## Interpreter Changes

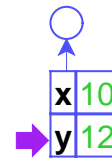
Same as before:

- Expressed values: Number + Proc
- Denoted values: Ref(Expressed Value)

The difference is that application doesn't always create a new location for a new variable binding

=> Separate *location* creation from *environment* extension

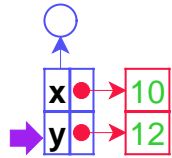
## Assignment and Call-by-Reference



The old way

```
let x = 10
  y = 12
  in +(x,y)
```

## Assignment and Call-by-Reference



The new way

```
let x = 10
    y = 12
in +(x,y)
```

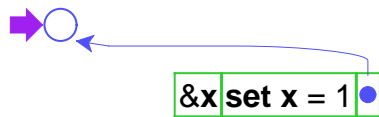
## Call-by-Reference



Do the previous evaluation the new way...

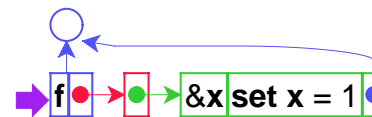
```
let f = proc(&x) set x = 1
in let y = 0
    in { (f y);
        y
    }
```

## Call-by-Reference



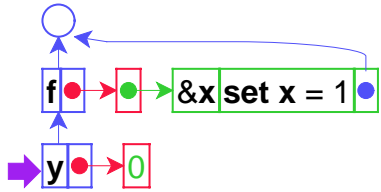
```
let f = proc(&x) set x = 1
in let y = 0
    in { (f y);
        y
    }
```

## Call-by-Reference



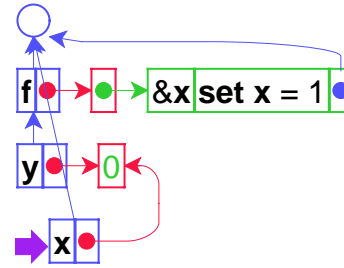
```
let f = proc(&x) set x = 1
in let y = 0
    in { (f y);
        y
    }
```

### Call-by-Reference



```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

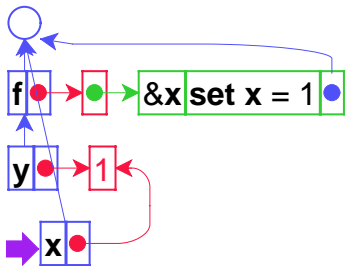
### Call-by-Reference



This time, the new environment frame points to a location box, which is consistent with other frames

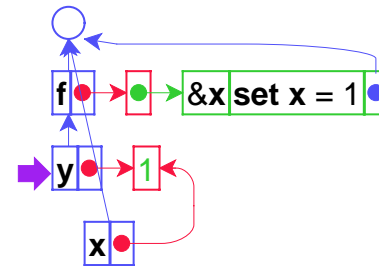
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  in let y = 0
    in { (f y);
        y
      }
```

### Call-by-Reference



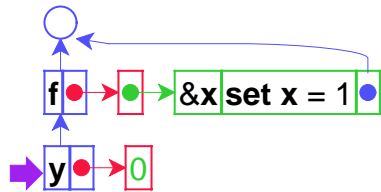
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    in { (f y);
        y
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```

### Call-by-Reference



```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f y);
        y
      }
```

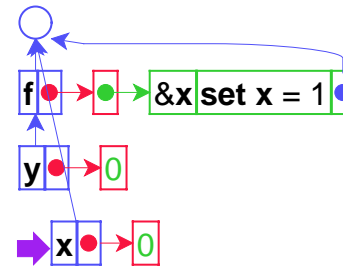
## Call-by-Reference with Non-variables



If call-by-reference argument is not a variable...

```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f 0);
        y
      }
```

## Call-by-Reference with Non-variables



... create a location

```
let f = proc(&x) set x = 1
  in let y = 0
    in { (f 0);
        y
      }
```

## Interpreter Changes

- Add call-by-reference arguments (indicated by &)
- New **var** datatype, with **cbv-var** and **cbr-var** variants
- Create explicit **locations** for variables
 

```
location : expval -> location
location-val : location -> expval
location-set! : location expval -> void
```
- Change variable lookup to de-reference locations
- Change **set** to work on locations
- Add **eval-fun-rands** and change **apply-proc**

## & versus \* in C++

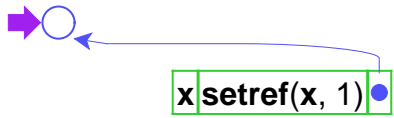
```
void f(int* x) {
  *x = 1;
}

int main() {
  int y = 0;
  f(&y);
  return y;
}
```

- This is back to **call-by-value**, but with a reference as a value
- To study this form of call, we can add explicit references to our language, too

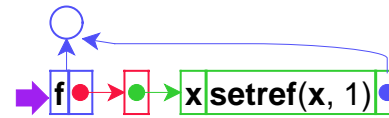


### Call-by-Value with References



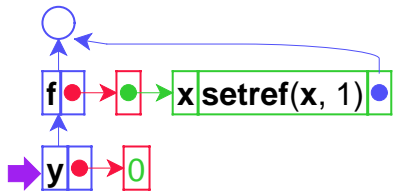
```
let f = proc(x) setref(x, 1)
in let y = 0
  in { (f ref(y));
      y
    }
```

### Call-by-Value with References



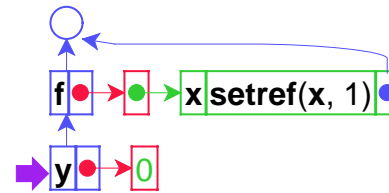
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let f = proc(x) setref(x, 1)
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  in { (f ref(y));
      y
    }
```

### Call-by-Value with References



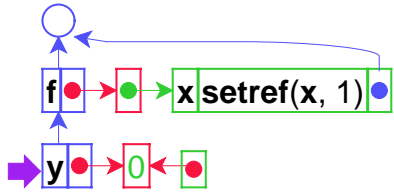
```
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in let y = 0
  in { (f ref(y));
      y
    }
```

### Call-by-Value with References



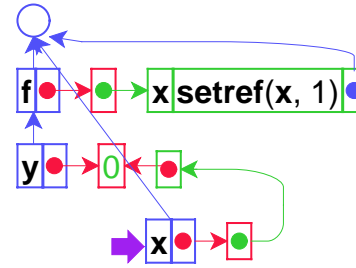
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```

### Call-by-Value with References



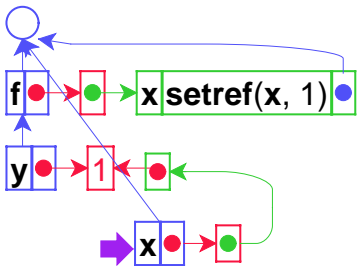
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```

### Call-by-Value with References



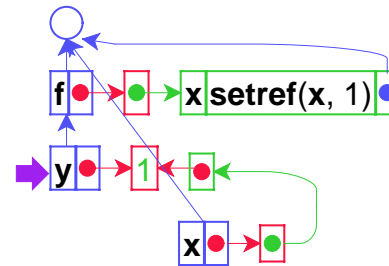
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### Call-by-Value with References



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### Call-by-Value with References



```
let f = proc(x) setref(x, 1)
in let y = 0
  in { (f ref(y));
      y
    }
```

## Interpreter Changes for References

Revised language:

- Expressed vals: Number + Proc + Ref(Expressed Val)
- Denoted vals: Ref(Expressed Val)

Interpreter changes:

- Add **reference** values
- Add **ref** form and **setref** primitive

## Lazy Evaluation of Function Arguments

```
let f = proc(x)0
in (f +(1,+(2,+(3,+(4,+(5,6))))))
```

The computed 21 is never used.

What if we were *lazy* about computing function arguments (in case they aren't used)?

## Lazy Evaluation of Function Arguments

One way to laziness:

```
let f = proc(xthunk)0
in (f proc()+ (1,+(2,+(3,+(4,+(5,6))))))
```

```
let f = proc(xthunk)-((xthunk), 7)
in (f proc()+ (1,+(2,+(3,+(4,+(5,6))))))
```

By using **proc** to delay evaluation, we can avoid unnecessary computation.

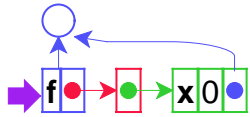
How about making the language compute function arguments lazily in *all* applications?

## Evaluation with Lazy Arguments



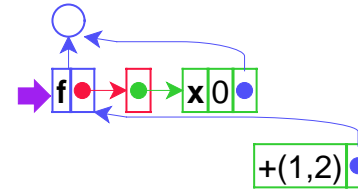
```
let f = proc(x)0
in (f +(1,2))
```

### Evaluation with Lazy Arguments



let f = proc(x)0  
in (f +(1,2))

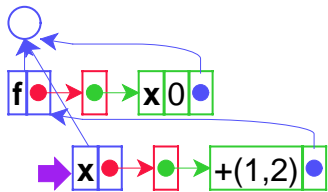
### Evaluation with Lazy Arguments



let f = proc(x)0  
in (f +(1,2))

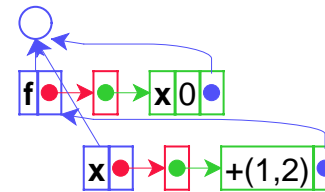
Application creates a new kind of green box, with two slots: a *thunk*

### Evaluation with Lazy Arguments



let f = proc(x)0  
in (f +(1,2))

### Evaluation with Lazy Arguments



let f = proc(x)0  
in (f +(1,2))

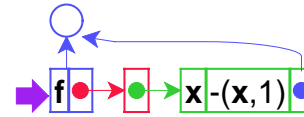
The result is 0

## Evaluation with Lazy Arguments



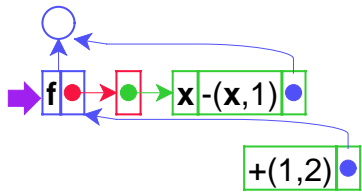
let f = proc(x)-(x,1)  
in (f +(1,2))

## Evaluation with Lazy Arguments



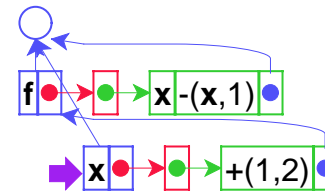
let f = proc(x)-(x,1)  
in (f +(1,2))

## Evaluation with Lazy Arguments



let f = proc(x)-(x,1)  
in (f +(1,2))

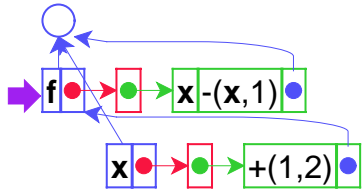
## Evaluation with Lazy Arguments



let f = proc(x)-(x,1)  
in (f +(1,2))

lookup of x...

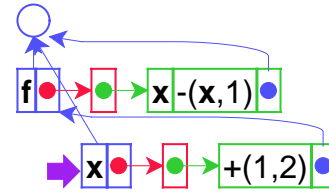
### Evaluation with Lazy Arguments



... forces evaluation of the thunk

```
let f = proc(x)-(x,1)
in (f +(1,2))
```

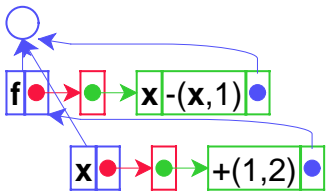
### Evaluation with Lazy Arguments



so 3 is the value of x

```
let f = proc(x)-(x,1)
in (f +(1,2))
```

### Evaluation with Lazy Arguments



The result is 2

```
let f = proc(x)-(x,1)
in (f +(1,2))
```

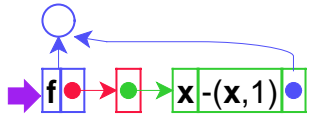
### Evaluation with Lazy Arguments



Lazy expression that needs its environment...

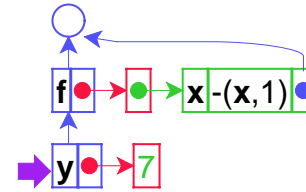
```
let f = proc(x)-(x,1)
in let y = 7
in (f +(1,y))
```

### Evaluation with Lazy Arguments



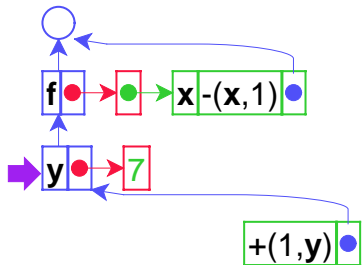
```
let f = proc(x)-(x,1)
  in let y = 7
    in (f +(1,y))
```

### Evaluation with Lazy Arguments



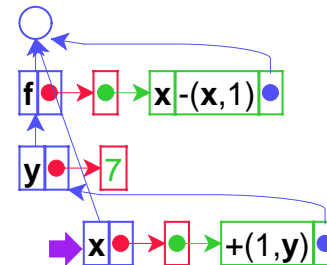
```
let f = proc(x)-(x,1)
  in let y = 7
    in (f +(1,y))
```

### Evaluation with Lazy Arguments



```
let f = proc(x)-(x,1)
  in let y = 7
    in (f +(1,y))
```

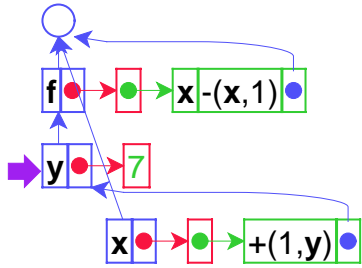
### Evaluation with Lazy Arguments



```
let f = proc(x)-(x,1)
  in let y = 7
    in (f +(1,y))
```

Evaluation of  $x$  forces the  
think...

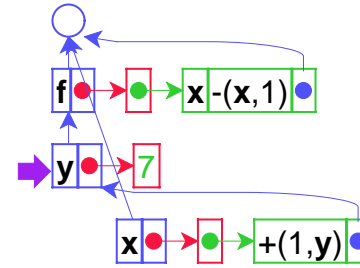
## Evaluation with Lazy Arguments



Triggering evaluation with the *think's* environment, not the current one

```
let f = proc(x)-(x,1)
  in let y = 7
     in (f +(1,y))
```

## Evaluation with Lazy Arguments



(The result will be 7)

```
let f = proc(x)-(x,1)
  in let y = 7
     in (f +(1,y))
```

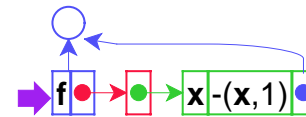
## Evaluation with Lazy Arguments



What if the right-hand side for *y* is an expression, instead of a value?

```
let f = proc(x)-(x,1)
  in let y = +(3,4)
     in (f +(1,y))
```

## Evaluation with Lazy Arguments

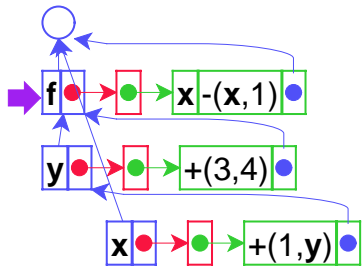


```
let f = proc(x)-(x,1)
  in let y = +(3,4)
     in (f +(1,y))
```





## Evaluation with Lazy Arguments



and so on (to get 7)

```
let f = proc(x)-(x,1)
  in let y = +(3,4)
    in (f +(1,y))
```

## Implementing Lazy Evaluation

Interpreter changes:

- Change `eval-fun-rands` to create thunks
- Change variable lookup to force thunk evaluation

(Implement in DrScheme)

## Call-by-Name and Call-by-Need

The lazy strategy we just implemented is *call-by-name*

- Advantage: unneeded arguments are not computed
- Disadvantage: needed arguments may be computed many times

```
let f = proc(x)+(x,+(x,x))
  in (f +(1,+(2,+(3,+(4,+(5,6))))))
```

Best of both worlds: *call-by-need*

- Evaluates each lazy expression once, then remembers the result

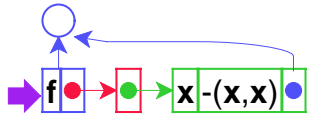
## Evaluation with Lazy Arguments



Start as before...

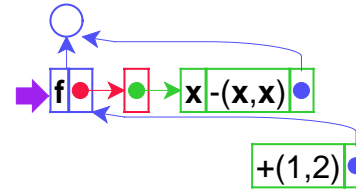
```
let f = proc(x)-(x,x)
  in (f +(1,2))
```

### Evaluation with Lazy Arguments



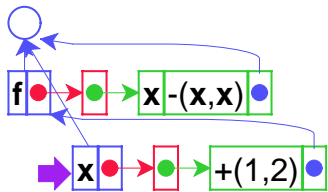
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### Evaluation with Lazy Arguments



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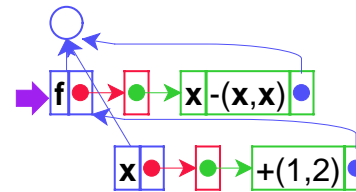
### Evaluation with Lazy Arguments



lookup of x...

let f = proc(x)-(x,x)  
in (f +(1,2))

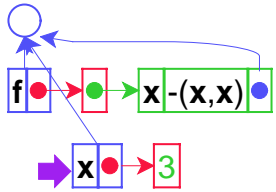
### Evaluation with Lazy Arguments



... forces evaluation of the thunk  
to get 3

let f = proc(x)-(x,x)  
in (f +(1,2))

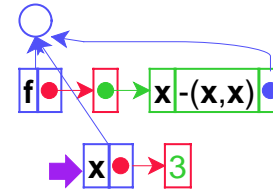
## Evaluation with Lazy Arguments



so change **x** to 3 --- which is the essence of call-by-need

```
let f = proc(x)-(x,x)
in (f +(1,2))
```

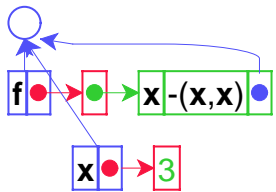
## Evaluation with Lazy Arguments



lookup of **x** again gets 3

```
let f = proc(x)-(x,x)
in (f +(1,2))
```

## Evaluation with Lazy Arguments



(The result is 0)

```
let f = proc(&x) set x = 1
in let y = 0
in { (f y);
y
}
```

## Implementing Call-by-Need

Interpreter changes:

- Change variable lookup to replace thunks in locations with their values

(Implement in DrScheme)

## Calling Convention Terminology

- Call-by-name and call-by-need = *lazy* evaluation
- Call-by-value = *eager* evaluation

Call-by-reference can augment either...

... but the combination of reference and laziness is difficult to reason about

## Popular Calling-Convention Choices

- Most languages are call-by-value
  - C, C++, Pascal, Scheme, Java, ML, Smalltalk...
- Some provide call-by-reference
  - C++, Pascal
- A few are call-by-need
  - Haskell
- Practically no languages are call-by-name

## Popularity of Laziness

Why don't more languages provide lazy evaluation?

- Disadvantage: evaluation order is not obvious

```
let x = 0 f = ...
in let y = set x=1
    z = set x=2
in { (f y z) ; x }
```

## Popularity of Laziness

Why do some languages provide lazy evaluation?

- Evaluation order does not matter if the language has no **set** form
- Such languages are called *purely functional*
  - Note: call-by-reference is meaningless in a purely functional language
- A language with **set** can be called *imperative*

## Laziness and Eageress

Even in a purely functional language, lazy and eager evaluation can produce different results

```
let f = proc(x)0
in (f [loop forever])
```

- Eager answer: none
- Lazy answer: 0