



# Mixing Typed and Untyped Code

A Tale of Proofs, Performance, and People

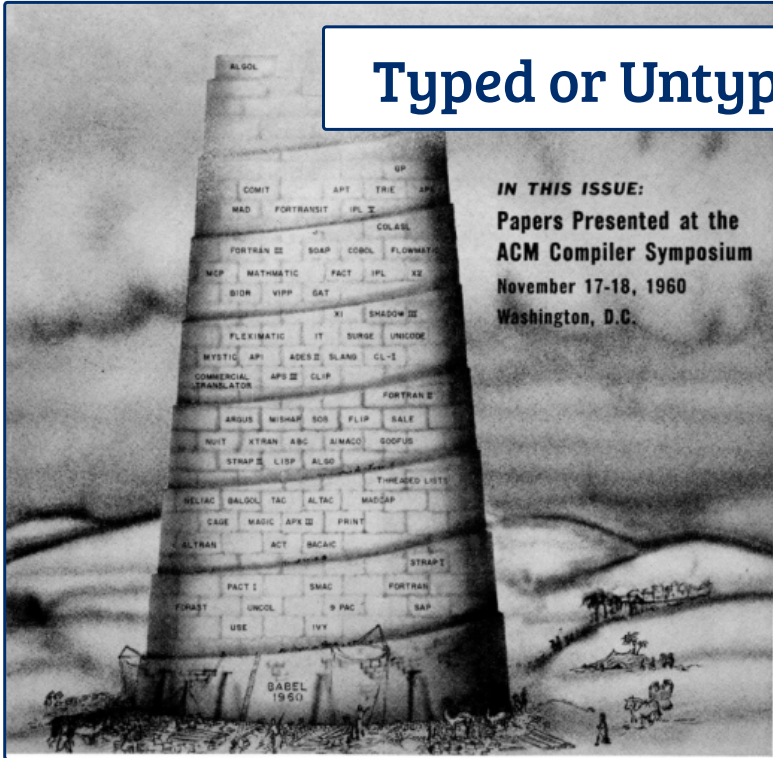


Ben Greenman  
Spring 2022



BROWN

# Typed or Untyped?





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Java is typed  
(statically typed)

```
HashMap<String, Integer> m =  
new HashMap<>();
```



JavaScript is untyped  
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var m = {}
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- + Prevent classes of bugs
- + Support tools



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Either way, **long-term implications** for  
development and maintenance



## Typed or Untyped



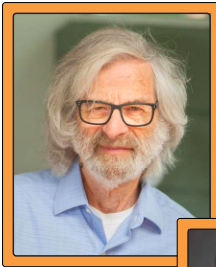
Strong support for both sides

## Typed or Untyped

T

U

Strong support for both sides



"The advantages of typed PLs are obvious"

Lamport & Paulson, TOPLAS 1999

## Typed or Untyped



Strong support for both sides

# Typed or Untyped

T

U

Strong support for both sides



Untyped PLs dominate on GitHub



1. Ruby



2. Python



3. JavaScript



4. PHP



5. Java

[s://madnight.github.io/githut/#/pull\\_requests/2021/4](https://madnight.github.io/githut/#/pull_requests/2021/4)

## X Typed or Untyped

T

U

**X** Typed or Untyped



**✓** Typed AND Untyped

**Gradual Typing**



## Gradual Typing



Key Motivation: **improve stable code** with types

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Key Motivation: **improve stable code** with types

```
function parse_lfd_chain(bv, pos, order, max_depth):  
    ....  
    tag_count = bv_ref(bv, pos, order)  
    next_offset = pos + 2 + (* tag_count 12)  
    next_pos = bv_ref(bv, next_offset, order)  
    pts = parse_tags(tag_count)  
    if next_pos == 0:  
        return pts  
    else:  
        return pts ++ parse_lfd_chain(bv, next_pos, order, max_depth - 1)
```



# Gradual Typing



Key Motivation: **improve stable code** with types

```
function parse_lfd_chain(bv, pos, order, max_depth):  
    function parse_lfd_chain(bv:Bytes, pos:Natural, order:Symbol, max_depth:Natural)  
        -> List[PTs]:  
        ....  
        tag_count = bv_ref(bv, pos, order)  
        next_offset = pos + 2 + (* tag_count 12)  
        next_pos = bv_ref(bv, next_offset, order)  
        pts = parse_tags(tag_count)  
        if next_pos == 0:  
            return pts  
        else:  
            return pts ++ parse_lfd_chain(bv, next_pos, order, max_depth - 1)
```

Document the parameters,  
benefit from type checks

## Gradual Typing

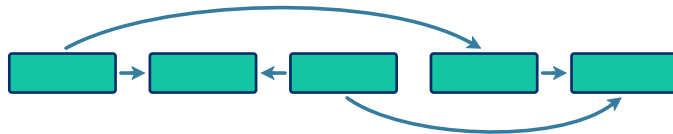


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## Gradual Typing



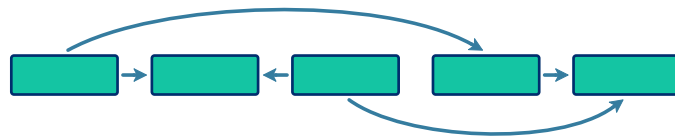
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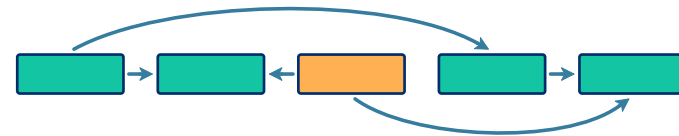
## Gradual Typing



Key Motivation: **improve stable code** with types



Add types to **one** component,  
leave the others **unchanged**



## Gradual Typing

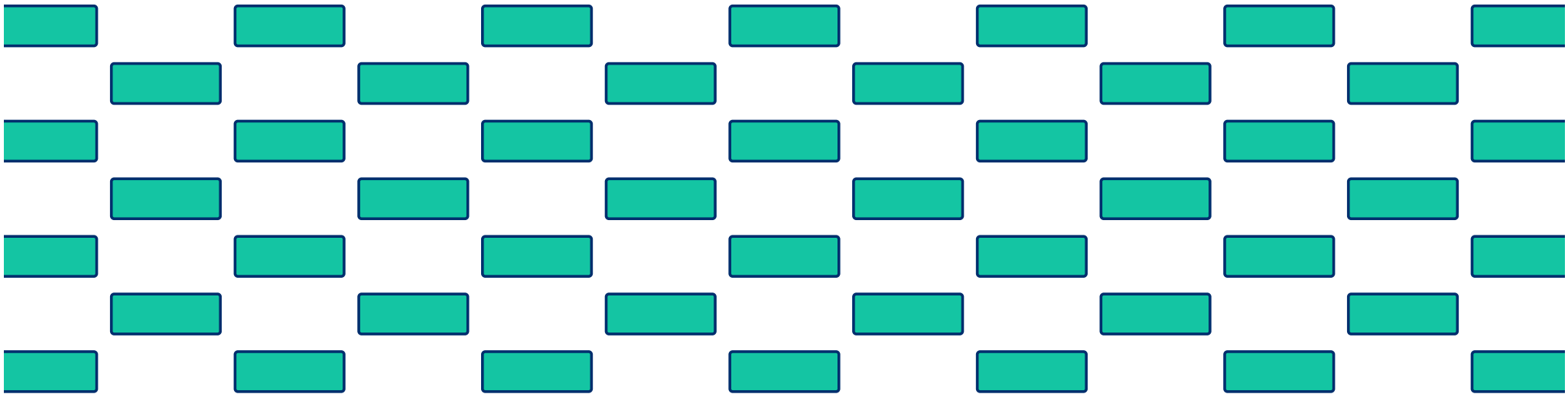


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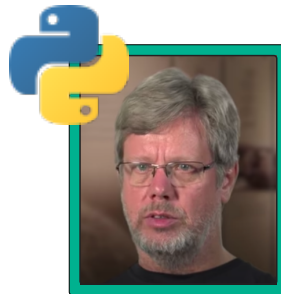
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# Gradual Typing



Key Motivation: **improve stable code** with types



"For **really large codebases**, static languages\*  
have their uses"

\* (despite all their visual overhead  
and compilation cycles and build tools)

## Gradual Typing





## Gradual Typing

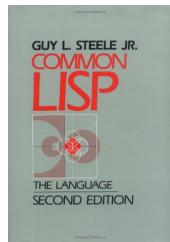


Active space!

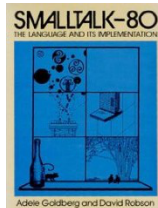
## Gradual Typing



Active space!



Common Lisp  
<1990

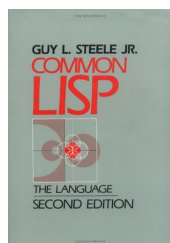


StrongTalk  
1993

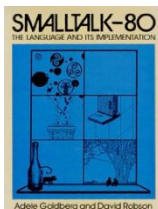
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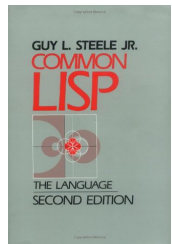


Gradual Typing  
2006

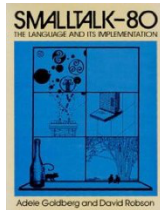
# Gradual Typing



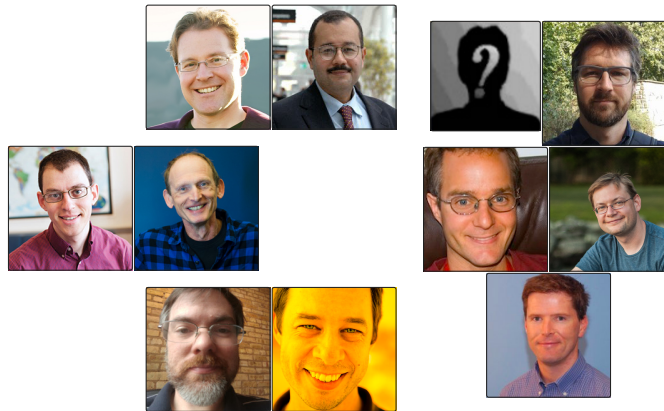
Active space!



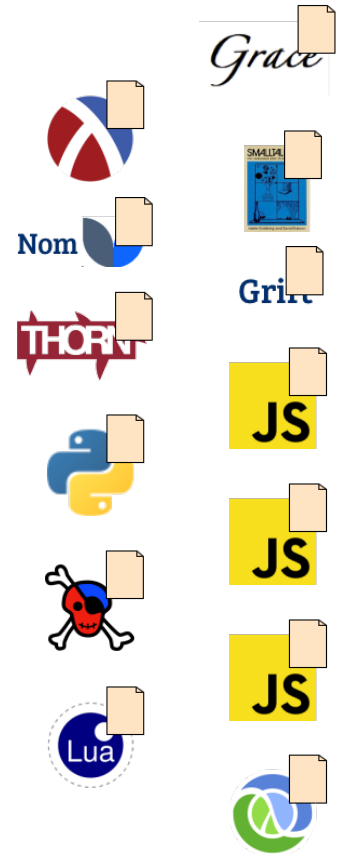
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Gradual Typing  
2006



+ Many Research PLs

## Gradual Typing



Active space!

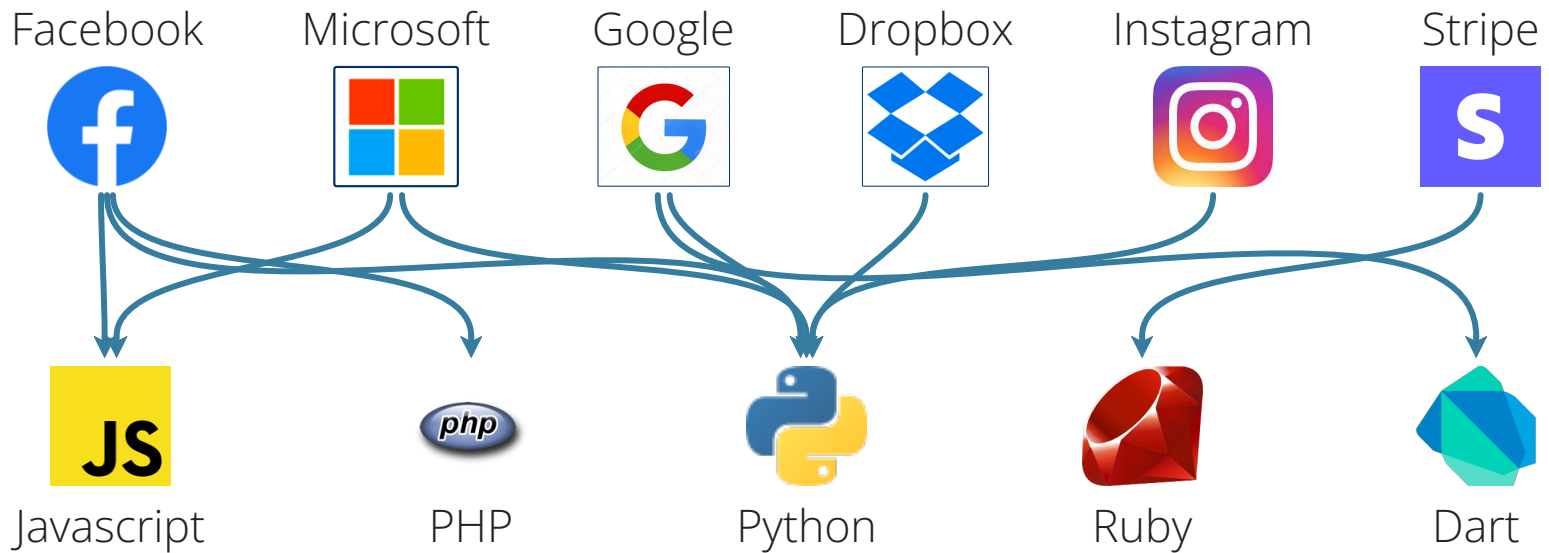
Major companies involved

# Gradual Typing



Active space!

Major companies involved



## Gradual Typing



Active space!

Major companies involved  
Growing community interest

# Gradual Typing



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DefinitelyTyped

The repository for high quality TypeScript type definitions



+ 8k interfaces

+ 5k contributors

+ 1 million clients



# Gradual Typing



Active space!

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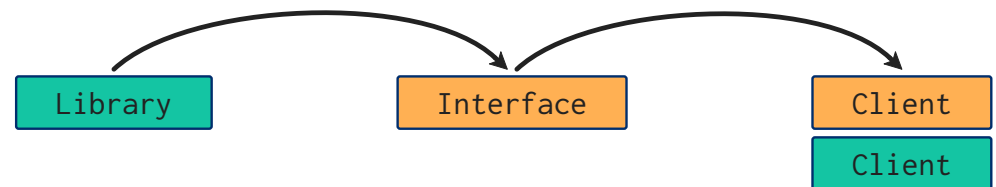
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**DT** DefinitelyTyped  
The repository for high quality TypeScript type definitions



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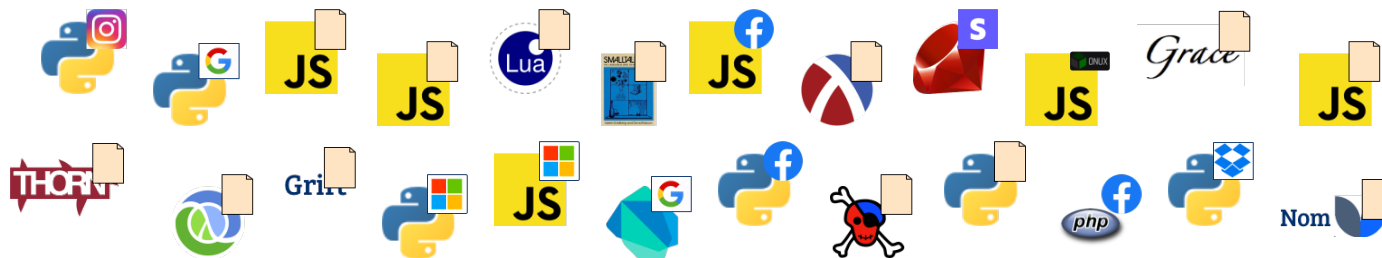
Common case: **new types** for **old libraries**



# Gradual Typing



So what's the **problem**?

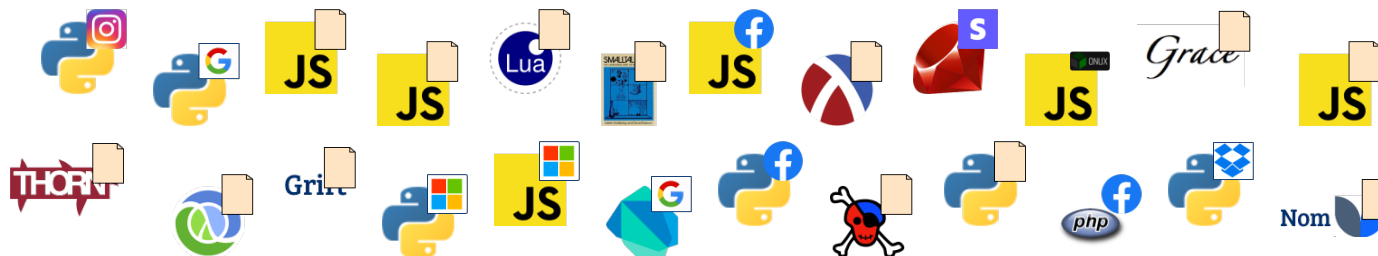


# Gradual Typing



So what's the **problem**?

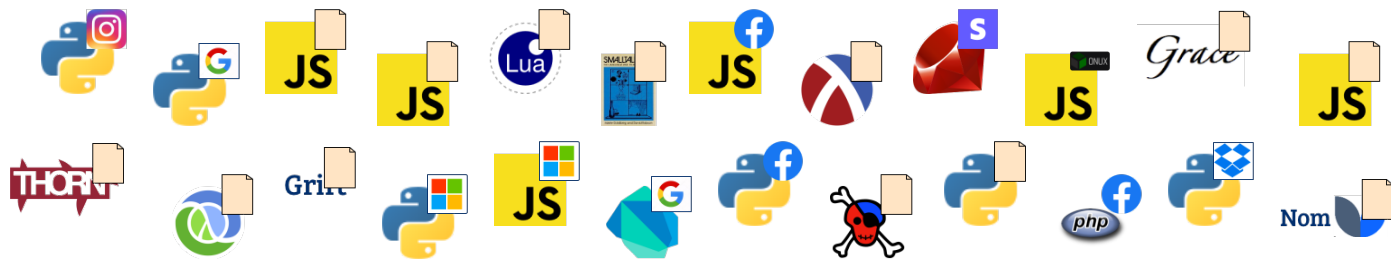
Lots of Languages, but also **Lots of Variety**



# Example 1

Typed Function

```
function add1(n : Num)  
  n + 1
```







## Example 1

Typed Function

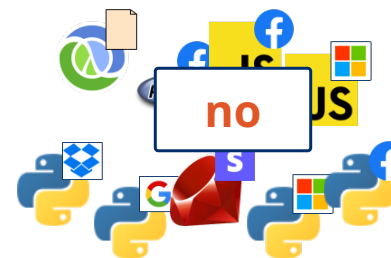
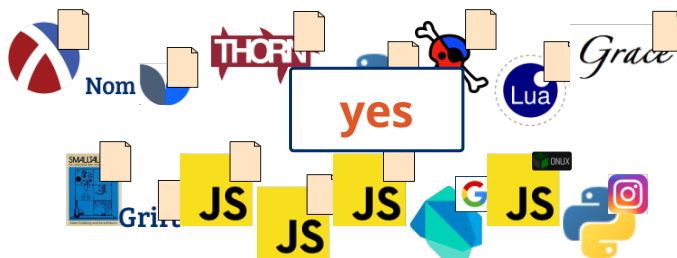
```
function add1(n : Num)  
  n + 1
```

Untyped Caller

```
add1("A")
```

Q. Is **n** really a number?

Some say **yes**, others say **no**







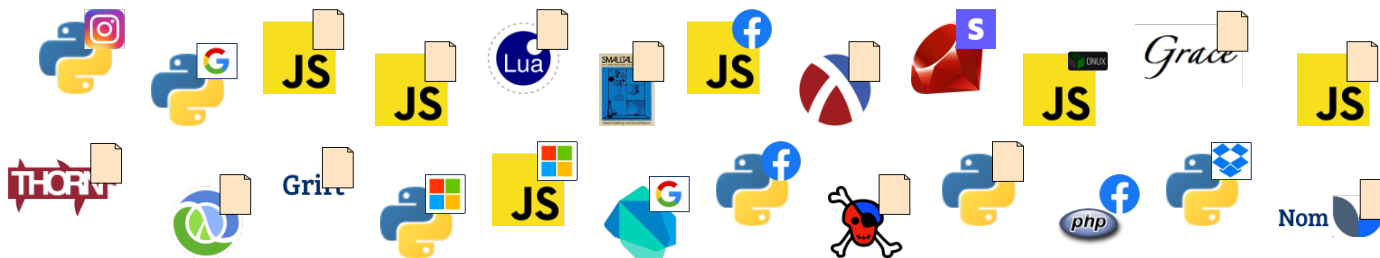
## Example 2

Untyped Array

```
arr = ["A", 3]
```

Typed Client

```
nums : Array(Num) = arr  
nums[0]
```



## Example 2

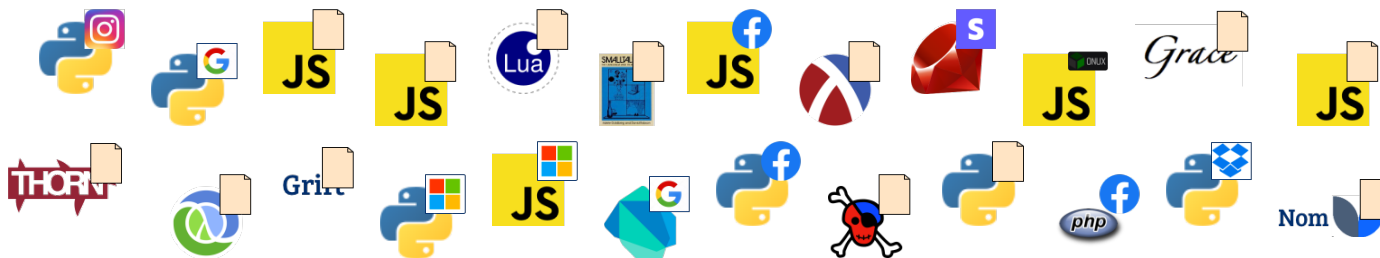
Untyped Array

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Q. Is **arr** an array of numbers?



## Example 2

Untyped Array

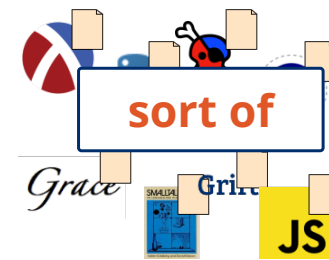
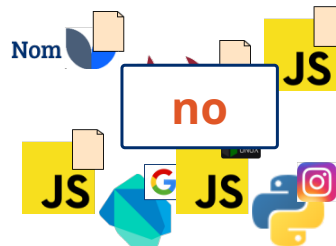
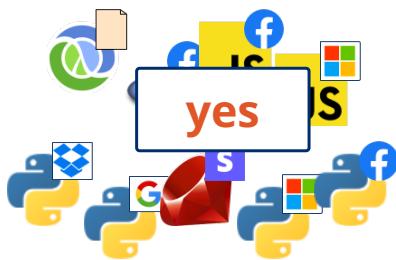
```
arr = ["A", 3]
```

Typed Client

```
nums : Array(Num) = arr  
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```

Q. Is **arr** an array of numbers?

Three common answers: **yes**, **no**, and **sort of**



## What Should Types Mean?

No consensus on basic questions!

Num

Array(Num)

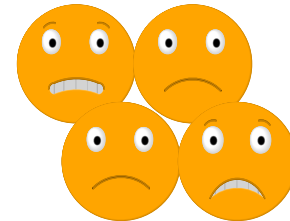
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Q. Did anyone **ask** programmers?



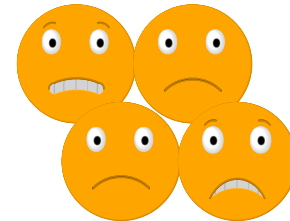
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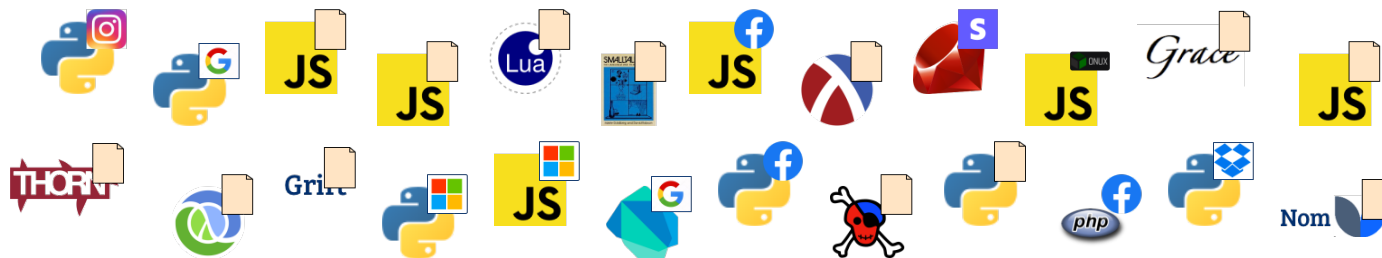
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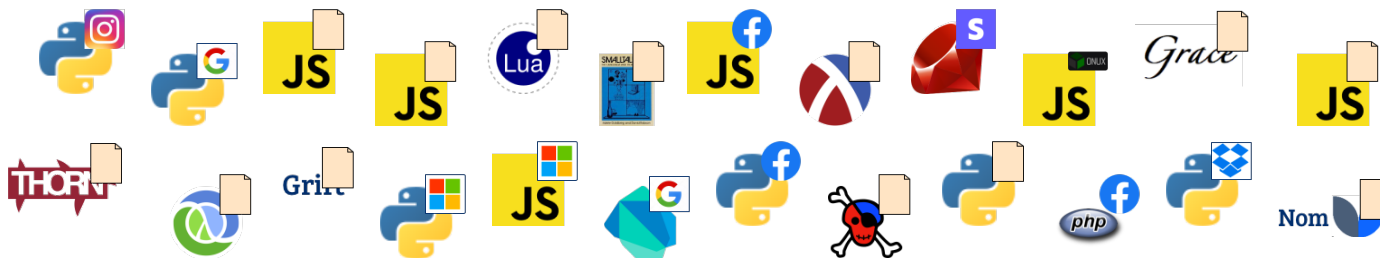
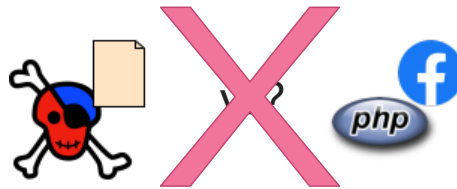


**Challenge:** How to compare languages?

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**Challenge:** How to compare languages?

Don't! Compare **semantics** instead.

ICFP '18



Proofs

T



U



**Challenge:** How to compare languages?

Don't! Compare **semantics** instead.

ICFP '18



**Proofs**

**T**



**U**

### **Guarded**

Types enforce behaviors

### **Transient**

Types enforce top-level shapes

### **Erasures**

Types enforce nothing

# Study: Behavior of Gradual Types

DLS '18



People

A **method** to compare semantics

## Study: Behavior of Gradual Types

DLS'18



People

```
arr = ["A", 3]
```

```
nums : Array(Num) = arr  
nums[0]
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A **method** to compare semantics

# Study: Behavior of Gradual Types

DLS'18



People

A **method** to compare semantics

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arr = ["A", 3]
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nums : Array(Num) = arr  
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(**G** says) Error: line 2

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DLS'18



People

A **method** to compare semantics

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Error: line 2

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"A"

Expected

Unexpected

|            | Like | Dislike |
|------------|------|---------|
| Expected   |      |         |
| Unexpected |      |         |

# Study: Behavior of Gradual Types

DLS'18



People

A **method** to compare semantics

- One program
- Distinct results
- Task: Label each result

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arr = ["A", 3]
```

```
nums : Array(Num) = arr  
nums[0]
```

- (G says) Error: line 2
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Expected

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# Study: Behavior of Gradual Types

DLS '18



People



Engineers



Students



Turkers



# Study: Behavior of Gradual Types

DLS '18



People



Engineers



Students



Turkers

How do the responses relate to the 3 **semantics**?

### Guarded

Types enforce behaviors

### Transient

Types enforce top-level shapes

### Erasure

Types enforce nothing

# Study: Behavior of Gradual Types

DLS '18



People



Engineers



Students



Turkers

Expected & Like



✓ **Guarded**

Types enforce behaviors

Unexpected & Dislike



✗ **Transient**

Types enforce top-level shapes



✗ **Erasure**

Types enforce nothing

## Case Closed?

✓ **Guarded**

Types enforce behaviors

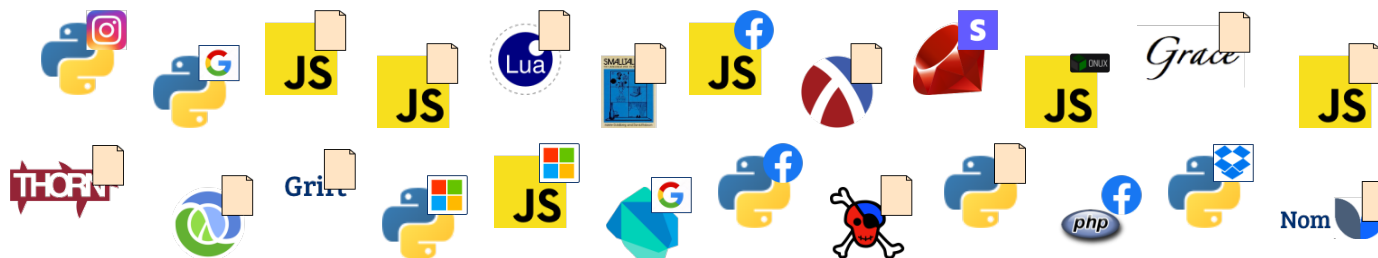
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Types enforce top-level shapes

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## Case Closed?



### ✓ Guarded

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### ✗ Transient

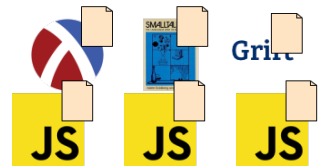
Types enforce top-level shapes

### ✗ Erasure

Types enforce nothing

# Case Closed? No!

Funny split ...



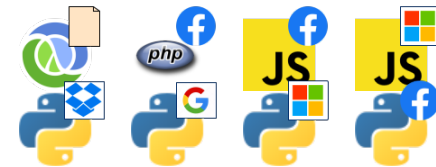
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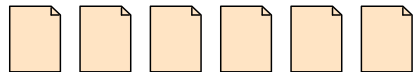
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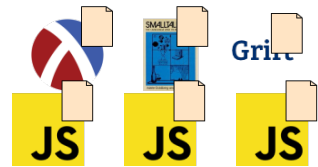
# Case Closed? No!

Funny split ...

Research Languages vs.

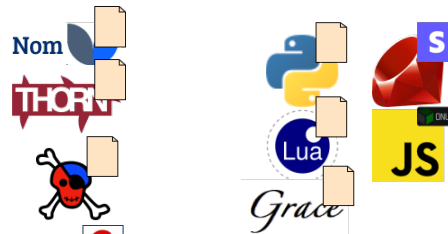


Popular Languages



✓ **Guarded**

Types enforce behaviors



✗ **Transient**

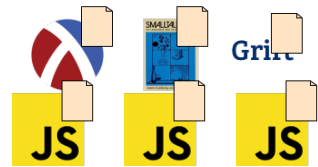
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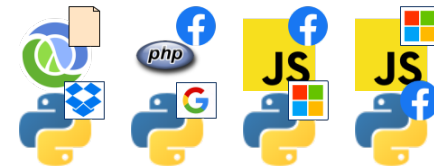
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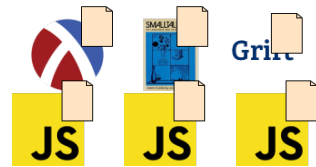
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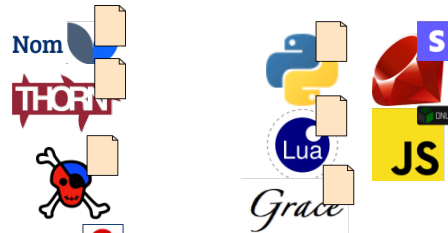
There are **two** problems:

- How should gradual types **behave**?
- What do behaviors **cost**?



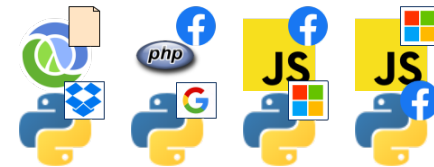
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## Where Do Costs Come From?

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```

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nums : Array(Num) = arr  
nums[0]
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(G says)

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Error: line 2
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(T says)

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```
"A"
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## Where Do Costs Come From?

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"A"
```

To detect an Error:

- **traverse** array at boundary
- or **wrap** and delay checks

Cost of **checks** can add up!

## Caution: Typed Racket



**Guarded** type guarantees, but **huge** worst-case costs

25x

180x

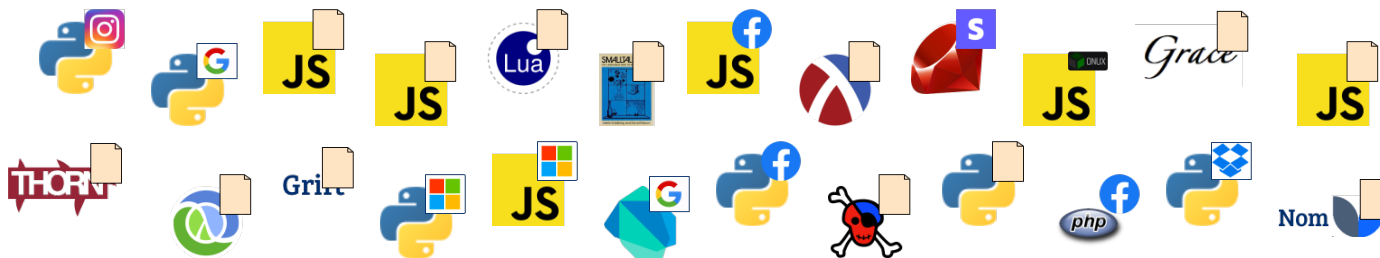
1400x

Q. Are bad points common, or rare?

Need a **method** to measure performance



**Performance**





## One Program, Many Points

What to Measure = **All** Gradual Possibilities

## One Program, Many Points

What to Measure = **All** Gradual Possibilities



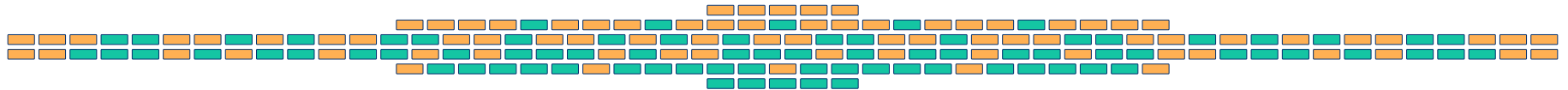
One program with **5** components ...

## One Program, Many Points

What to Measure = **All** Gradual Possibilities



One program with **5** components ...



... leads to **32** gradual points

In general, **N** components => **2<sup>N</sup>** points

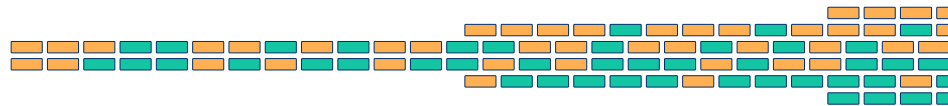


## One Program, Many Points

What to Measure = **All** Gradual Possibilities



One program with **5** components ...



**Challenge:** How to analyze the data?

... leads to **32** gradual points

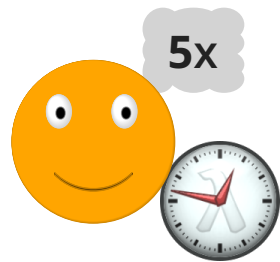
In general, **N** components => **2<sup>N</sup>** points

## Performance Insight

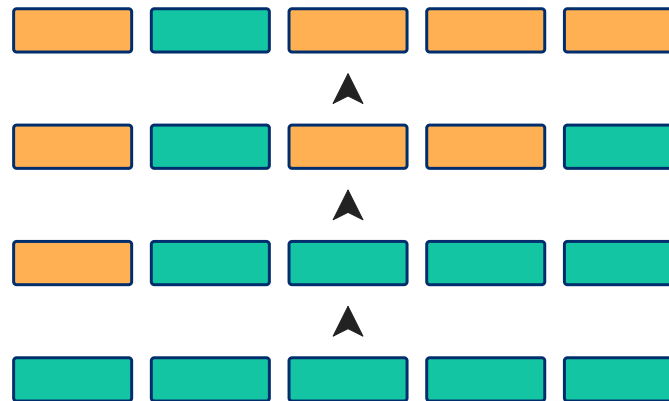
**Challenge:** How to analyze the data?

Focus on **D-deliverable** configurations

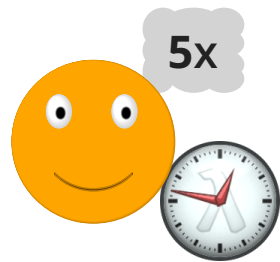
## D-deliverable: The Idea



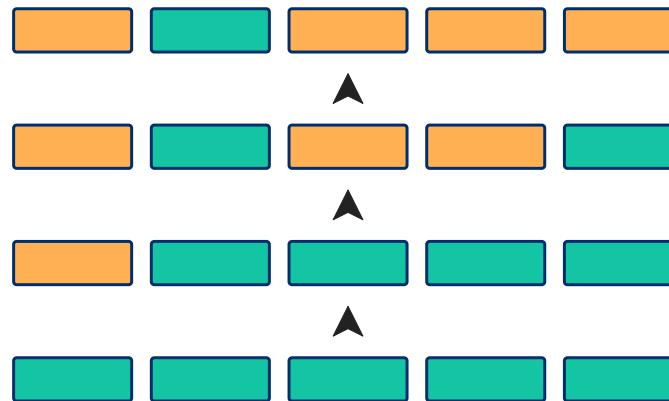
Are we *fast enough*?



## D-deliverable: The Idea



Are we *fast enough*?

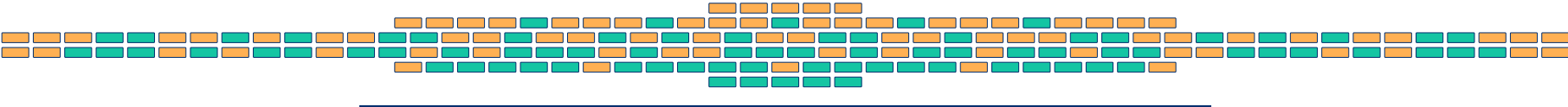


**Worst-case** overhead is **not** important

**Dx** slower is the upper bound

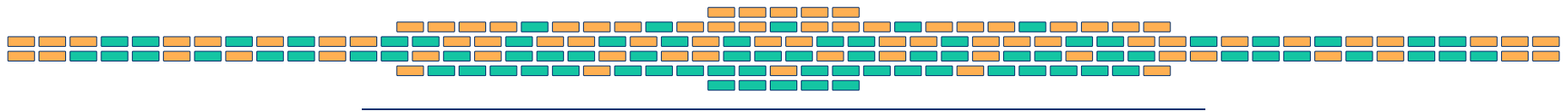
**D-deliverable:**

**How to Use**



## D-deliverable:

## How to Use



Compress to a **proportion** ...

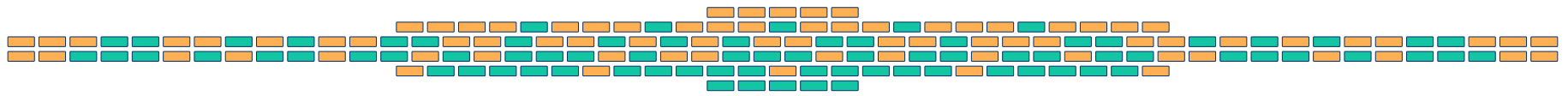
**D = 2**



**50%**

## D-deliverable:

## How to Use



Compress to a **proportion** ...

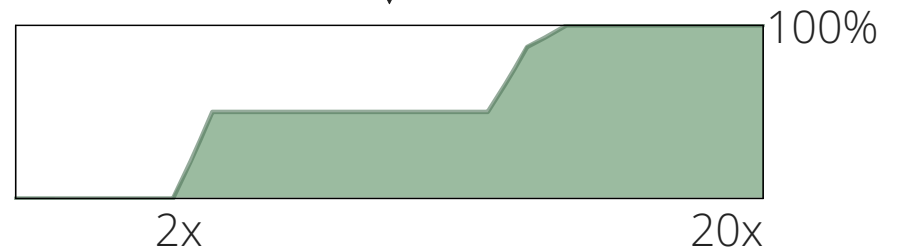
$$D = 2$$



**50%**

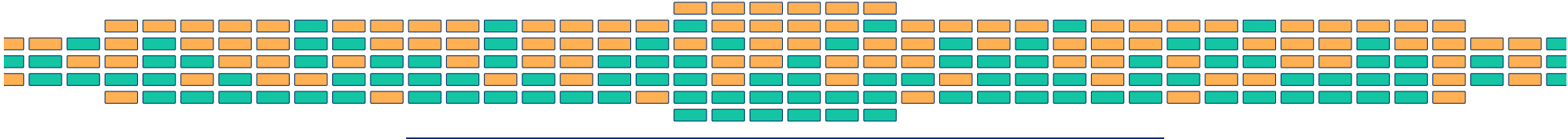
... or to a **CDF**

$$D \in [1, 20]$$



**D-deliverable:**

**How to Scale**



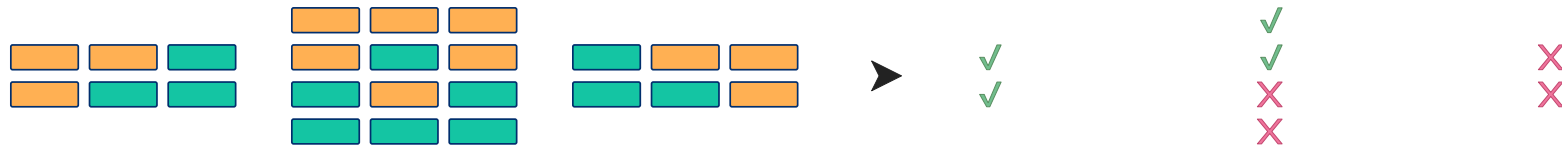


## D-deliverable:

## How to Scale

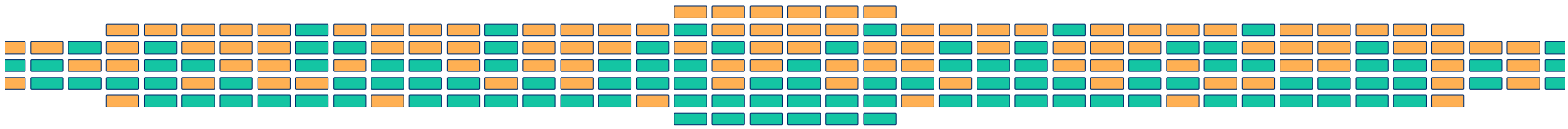


Choosing **D** enables a **Bernoulli random variable**

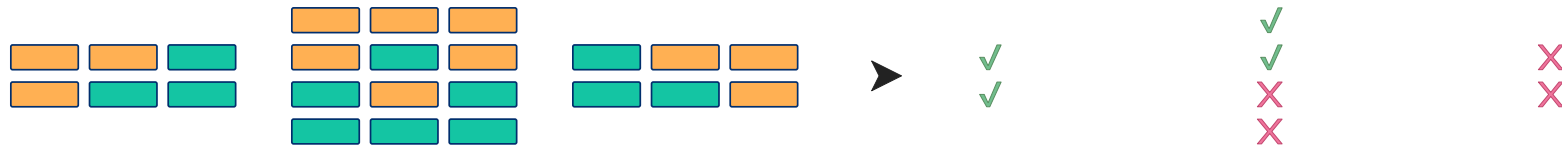


## D-deliverable:

## How to Scale



Choosing **D** enables a **Bernoulli random variable**



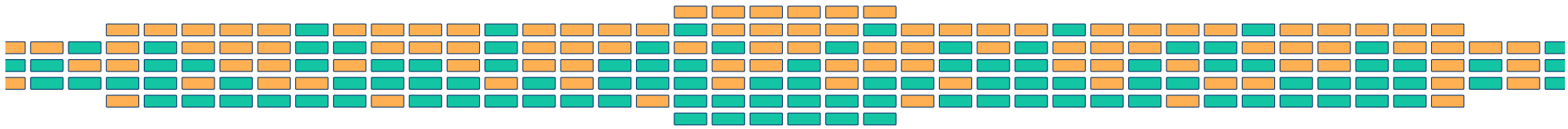
If 50% of **all points** are **D**-deliverable

=>

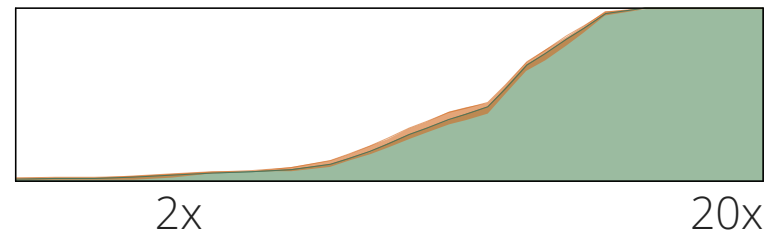
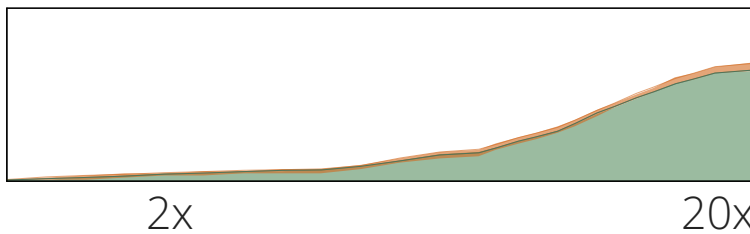
A **random point** has a 50% chance of being fast enough

## D-deliverable:

## How to Scale



Linear sampling has been effective  
for **approximating** the **true proportion**



(**Orange intervals** surround the two **green curves**)

## Method

1. Collect benchmark programs
2. Measure all configurations  
**or** a linear number of samples
3. Focus on the **D-deliverable** configurations



Larger Area = Better Performance

# Applications



Typed Racket

POPL '16

JFP '19

OOPSLA '18



Reticulated Python

PEPM '18

# Applications

Curated benchmarks for two languages



## Typed Racket

POPL '16

JFP '19

OOPSLA '18

The screenshot shows the documentation for the 'acquire' benchmark in Typed Racket. It includes a search bar, navigation links, a table of contents, and the main content area. The main content area contains the author's name (Matthias Felleisen), the source (github.com/mfelleisen/Acquire), dependencies (None), and a description: 'Simulates a board game between player objects. The players send messages to an administrator object; the administrator enforces the rules of the game.' Below the text is a diagram of a board game with 10 numbered nodes (0-9) and directed edges. A list of files is provided at the bottom: 0. admin.rkt, 1. auxiliaries.rkt, 2. basics.rkt, 3. board.rkt, 4. main.rkt, 5. player.rkt, 6. state.rkt, 7. strategy.rkt, 8. tree.rkt, and 9. .../base/untyped.rkt. The URL docs.racket-lang.org/gtp-benchmarks is displayed at the bottom.



## Reticulated Python

PEPM '18

The screenshot shows the 'Gradual Typing Across the Spectrum' website. It features a navigation bar with a GitHub logo and the title 'Gradual Typing Across the Spectrum'. Below the navigation bar is a red banner with the word 'Benchmarks' and a grey banner with 'Reticulated Python'. The main content area contains a link to the GitHub repository: [https://github.com/nuprl/retic\\_performance?path=benchmarks](https://github.com/nuprl/retic_performance?path=benchmarks). Below the link is a paragraph of text: 'Suite of Python programs adapted from: case studies reported by Vitousek, Kent, Siek, and Baker; the module-level evaluation of Big Types in Little Runtime; and open-source programs. Each function in these benchmarks may be typed or untyped. In other words, for a program with 10 functions the benchmark explores 1024 configurations of gradual typing.' Below the text is a section titled 'Appeared in:' with a bullet point: 'On the Cost of Type-Tag Soundness. Ben Greenman and Zeina Migeed. PEPM 2018'. The URL nuprl.github.io/gtp/benchmarks is displayed at the bottom.

from GitHub, Racket packages, Python benchmarks, ... usually without types

# Applications



Typed Racket

POPL '16

JFP '19

OOPSLA '18

- **Guarded** semantics
- Bad news! Most **over 20x**
- Better today, but still slow



Reticulated Python

PEPM '18

# Applications



Typed Racket

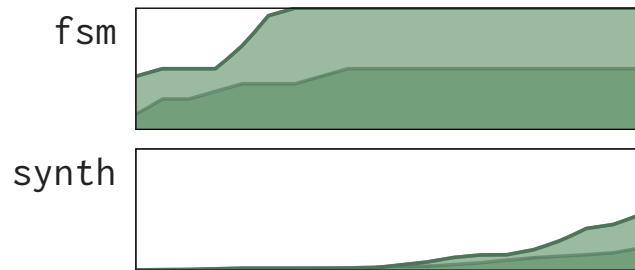
POPL '16

JFP '19

OOPSLA '18

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Example: 2015 to 2020



Reticulated Python

PEPM '18



# Applications



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JFP '19

OOPSLA '18

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Reticulated Python

PEPM '18

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- Not bad! All **under 10x**

# Applications



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# Applications



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Reticulated Python

PEPM '18

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- Not bad! All **under 10x**

Q. Are **Guarded** and **Transient** "equally" type-sound?

Need a **method** to assess type guarantees



**Proofs**

Q. Are **Guarded** and **Transient** "equally" type-sound?

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**Type Soundness** (TS) is the standard property for typed languages  
"typed code agrees with the types"

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... but our survey says they're different



✓ **Guarded**



✗ **Transient**

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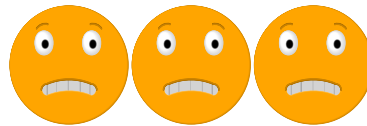
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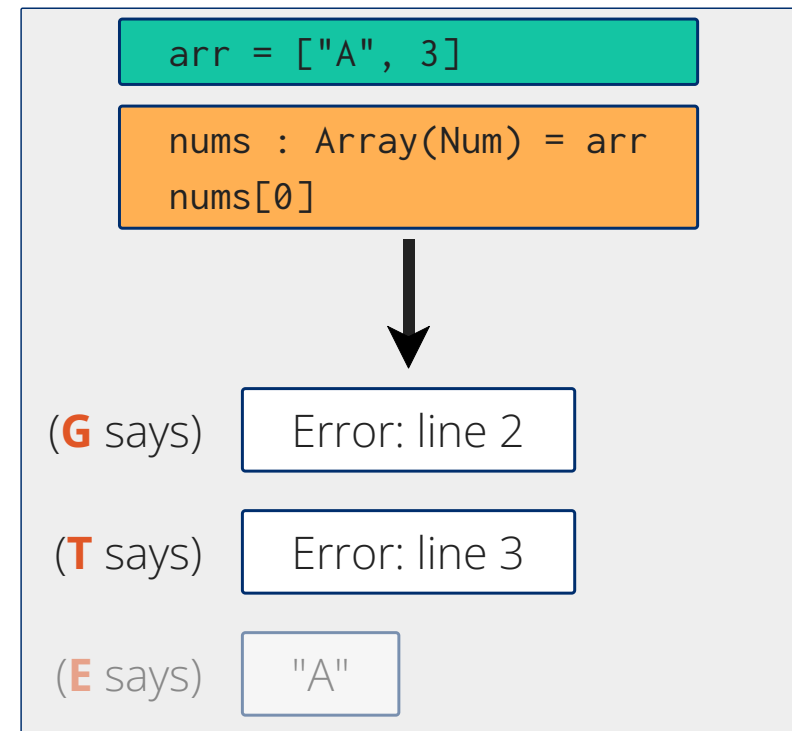
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## From TS to CM

00PSLA'19

In Submission'22

Both **Guarded** and **Transient** satisfy **type soundness** (TS)

Only **Guarded** satisfies **complete monitoring** (CM)

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arr = ["A", 3]
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```
nums : Array(Num) = arr
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nums[0]
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**G**

Error: line 2

**T**

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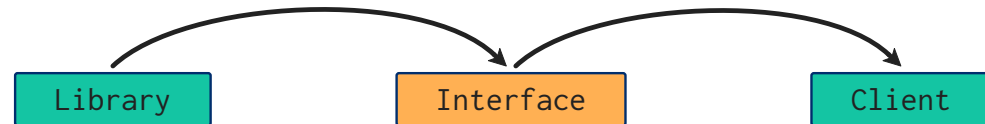


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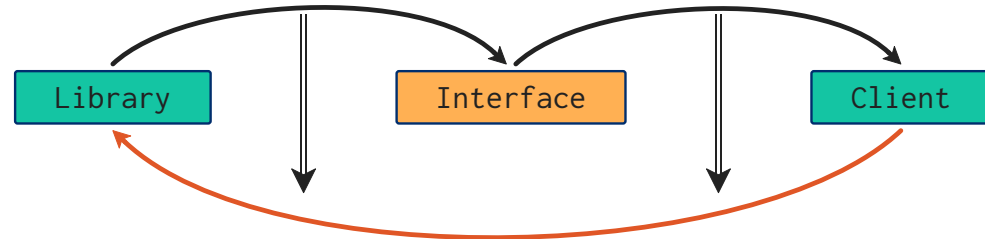
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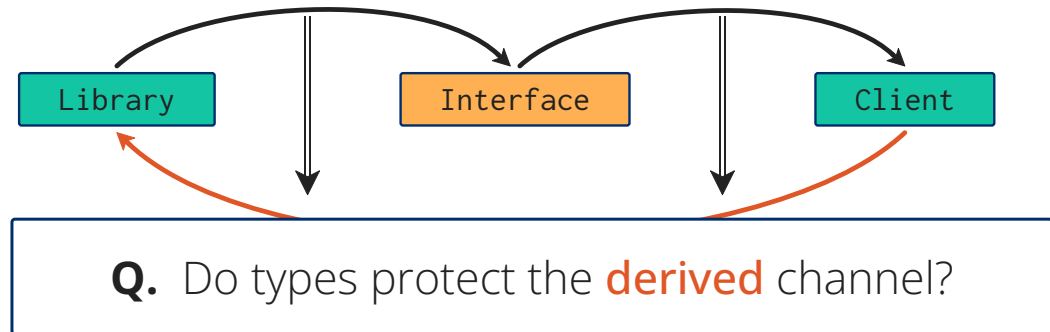
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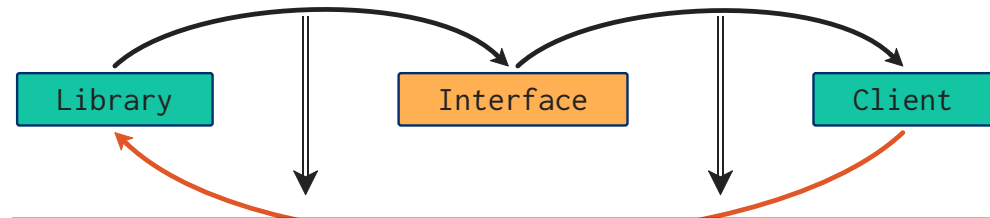
```
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```

```
nums[0]
```



**G** Error: line 2

**T** "A"



Q. Do types protect the **derived** channel?

**Guarded** (CM+TS): **Yes**  
types made the channel

**Transient** (TS): **No**  
channel is untyped to untyped

# Applications



Typed Racket



Reticulated Python



# Applications



Typed Racket



Reticulated Python

Q. Are **Guarded** and **Transient** types equally *strong*?

# Applications



Typed Racket



Reticulated Python

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No!

# Applications



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No!

**Challenge:** Can the two interoperate?

# Applications



Typed Racket



Reticulated Python

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No!

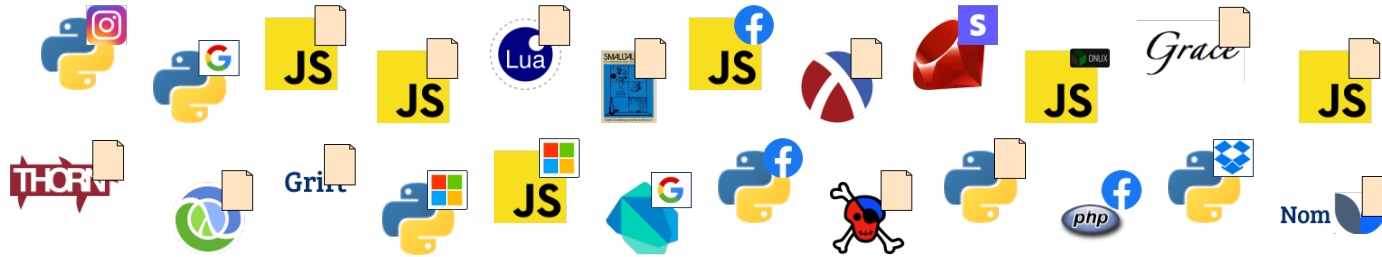
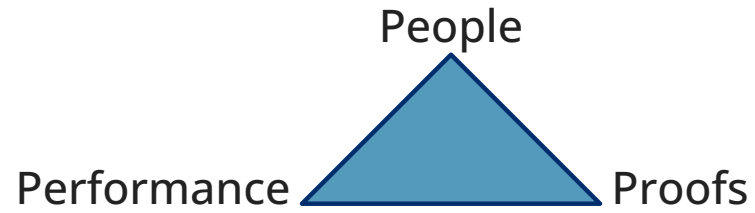
**Challenge:** Can the two interoperate?

Yes, **Deep+Shallow** Racket

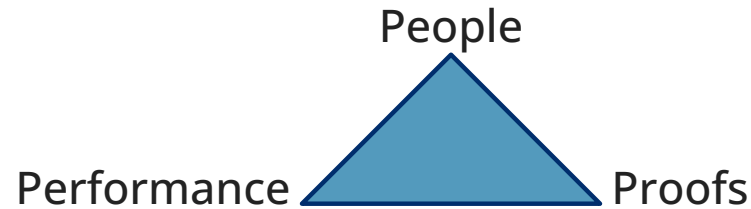
PLDI '22



# Foundations for Gradual Languages



# Foundations for Gradual Languages

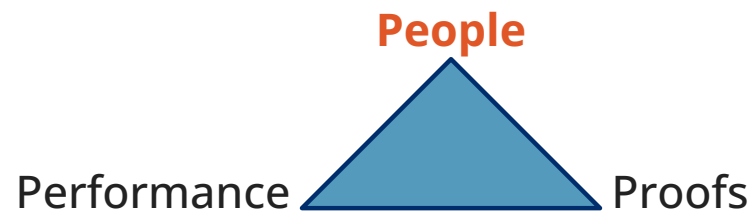


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**Research Contributions:**

- Characterizing Designs
- Directing Improvements
- Inspiring New Languages

## Ongoing Work

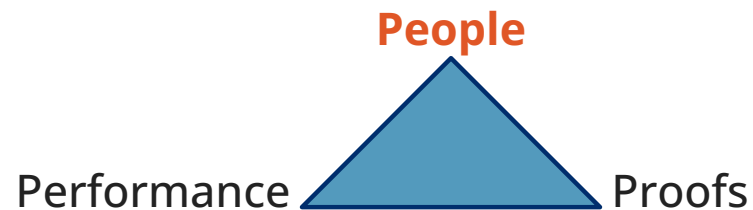


## Ongoing Work

### Static Python at Instagram

Few types, but fast performance

Gradual soundness: type guarantees vs. ease-of-use





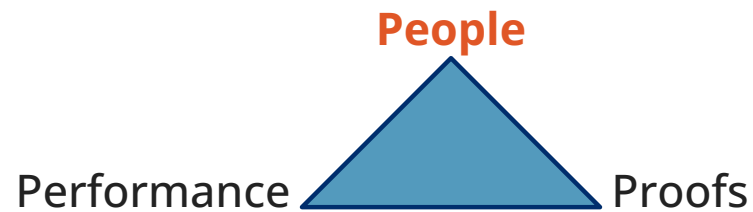
## Ongoing Work

Static Python   
Gradual Soundness



### Rational Programmer

A method for PL pragmatics  
Humans out-of-the-loop



## Ongoing Work

Static Python   
Gradual Soundness

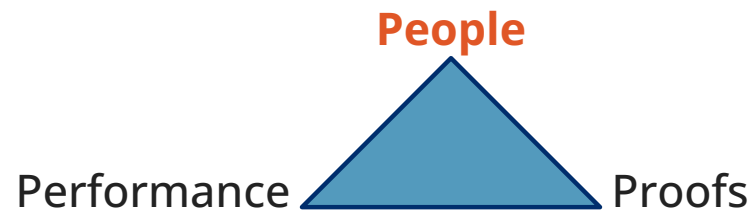


Rational Programmer  
Directly measure pragmatics

### Human Factors for Formal Methods:

Language levels for **Alloy**

**LTL** misconceptions (next slide)



# LTL Misconceptions

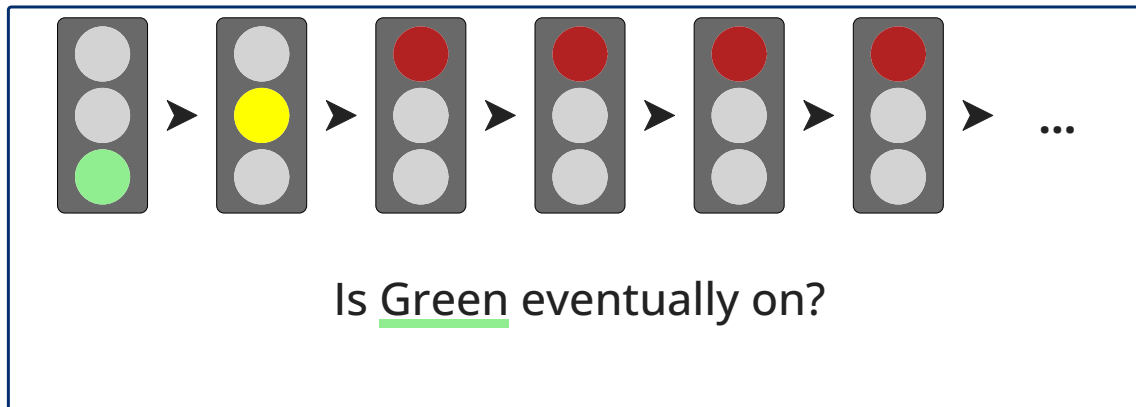
Linear Temporal Logic

used in: **verification**, **synthesis**, and **robot planning**

## LTL Misconceptions

Linear Temporal Logic

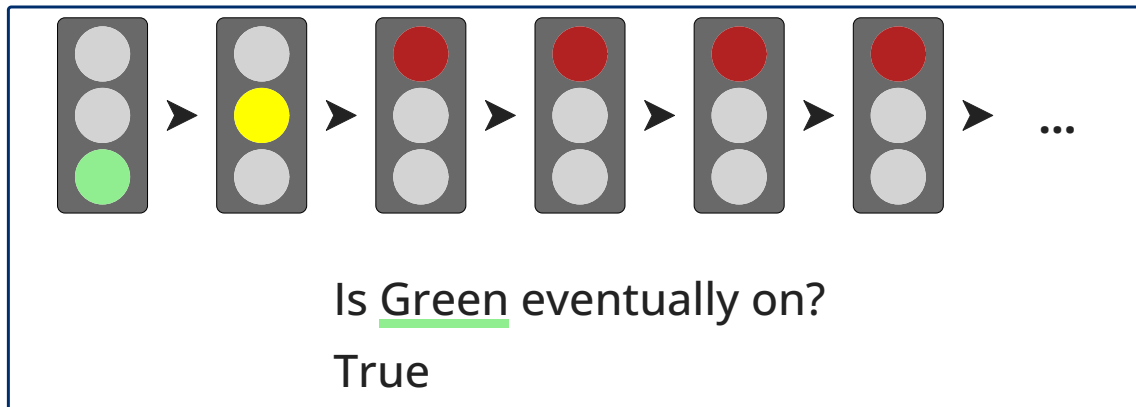
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## LTL Misconceptions

Linear Temporal Logic

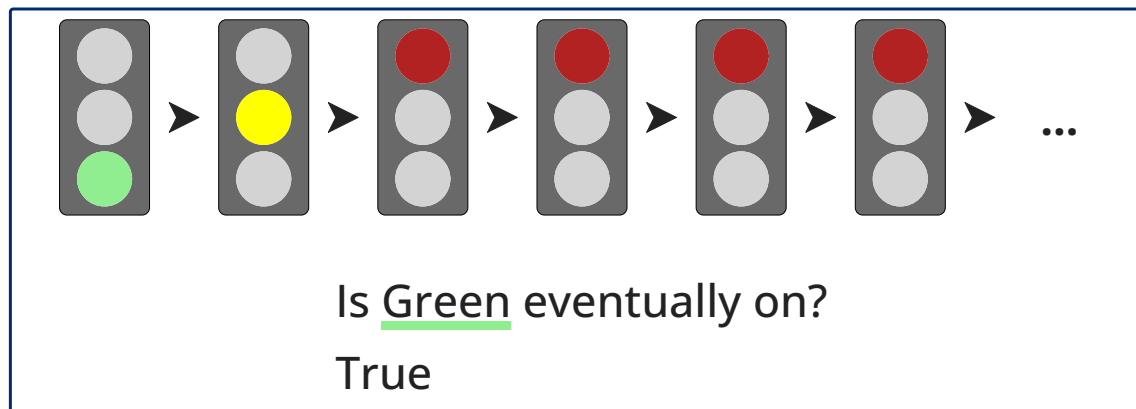
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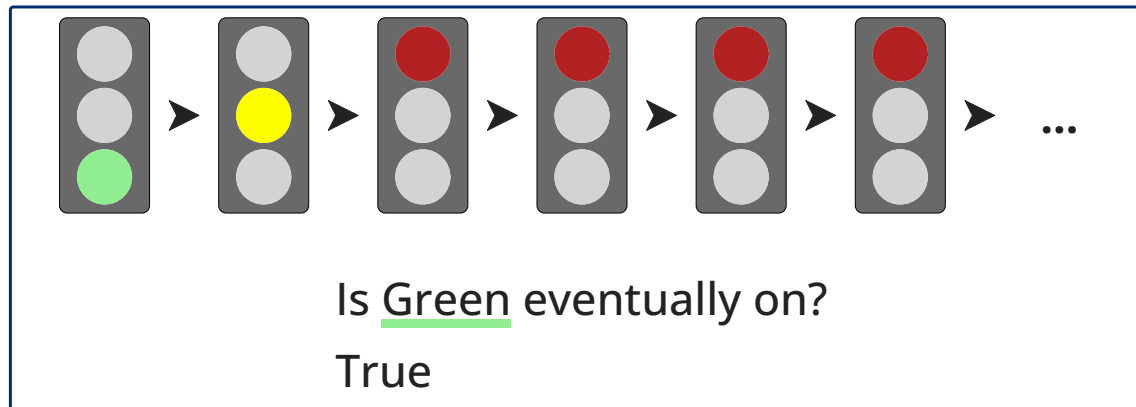
Q. **In what ways** is LTL tricky, and **what can we do** about it?

Studies with researchers & students

## LTL Misconceptions

Linear Temporal Logic

used in: **verification**, **synthesis**, and **robot planning**



Q. **In what ways** is LTL tricky, and **what can we do** about it?

Studies with researchers & students

Early outcome: **Better syntax** for Alloy 6

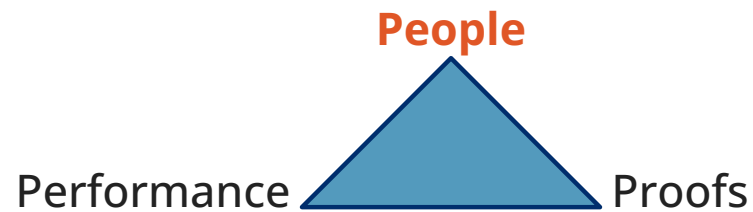
## Ongoing Work

Static Python   
Gradual Soundness



Rational Programmer  
Directly measure pragmatics

Human Factors for FM  
Alloy and LTL







## Future Work

## Future Work

Typed + Untyped is a **multi-language** problem



- 2 similar languages
- higher-order interoperability
- **strong** vs. **weak** invariants

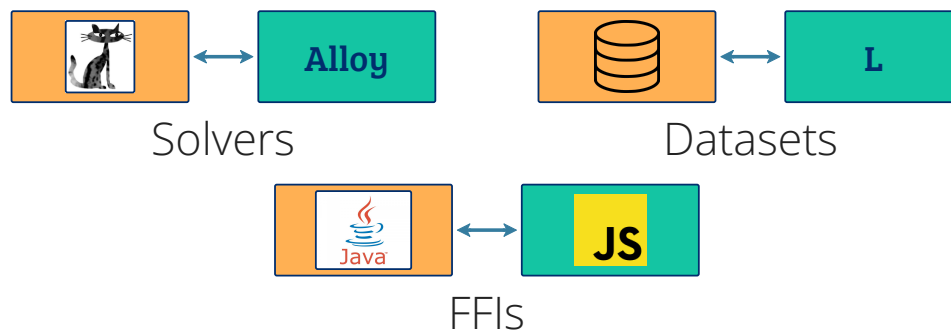


## Future Work

**Multi-language systems** are everywhere!

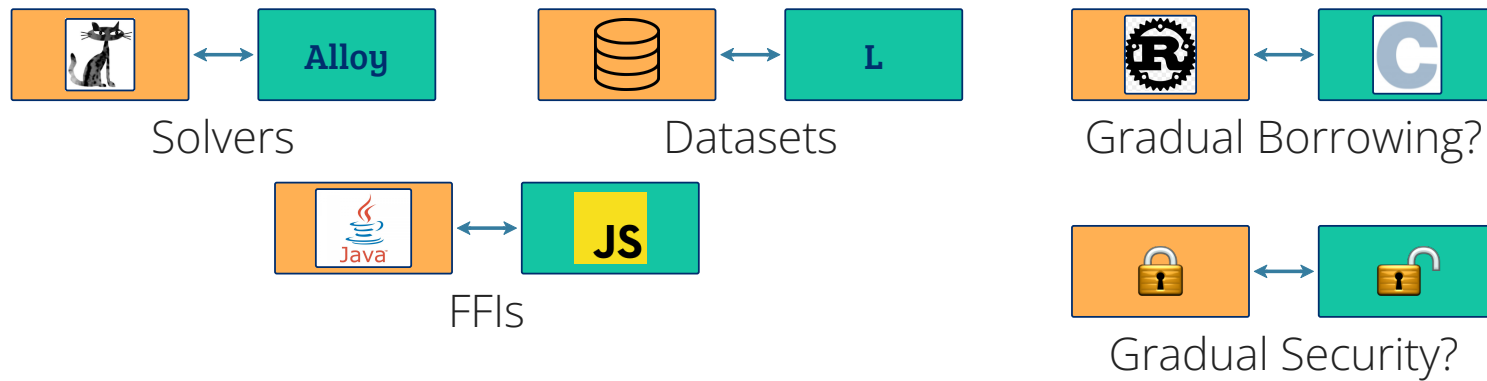
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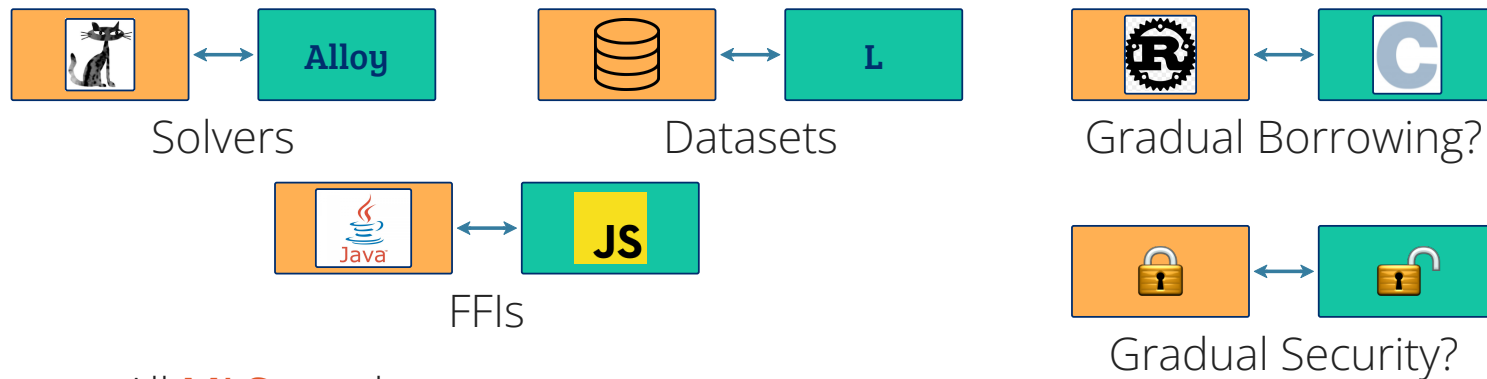
## Future Work

Multi-language systems are everywhere!



## Future Work

Multi-language systems are everywhere!



All **MLS** need:

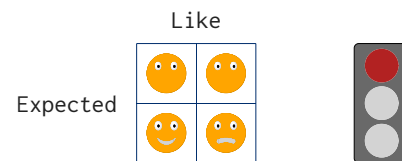
- **Expressive** Boundaries
- **Correct & Fast** Validation





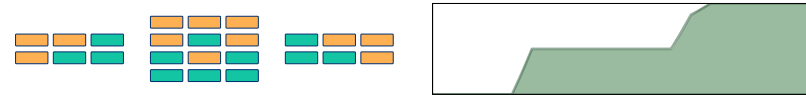
## People

Behavior of Gradual Types  
Human Factors for Formal Methods



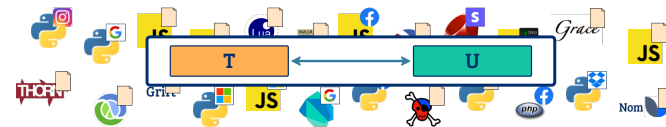
## Performance

Measuring Costs at Scale

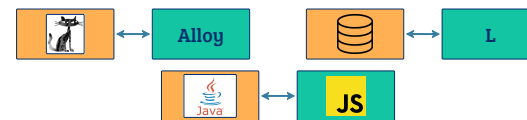


## Proofs

Comparing Type Guarantees



Methods for **multi-language systems**







## Teaching Alloy

Alloy is a **modeling language** that comes with **two styles**:

### Predicate

```
all a, b, c: univ |  
  a->b in f and b->c in f  
  implies a->c in f
```

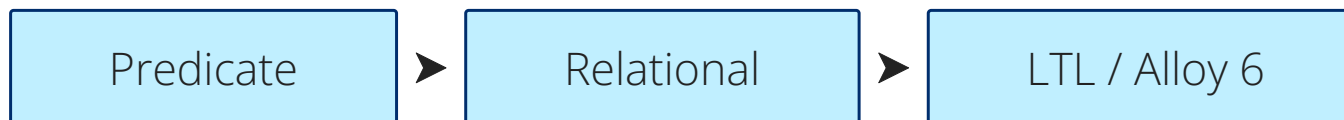
### Relational

```
f.f in f
```

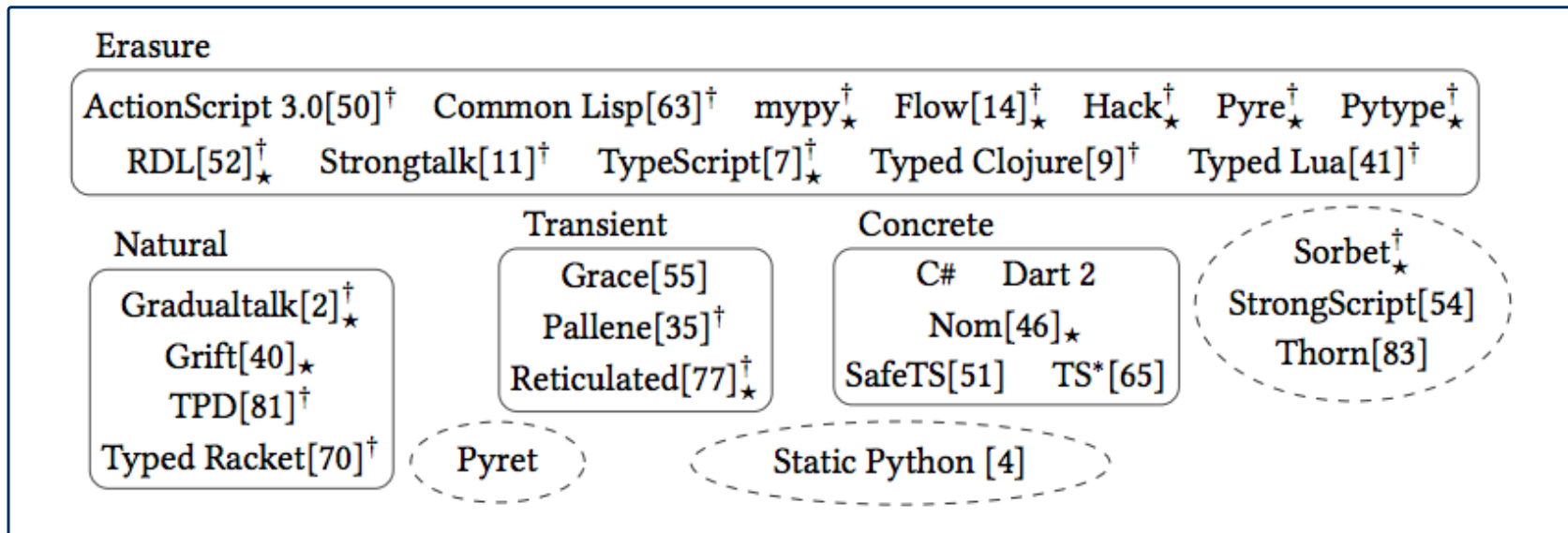
(f is transitive)

**Problem:** errors assume you know both styles!

Q. Can **language levels** give a smooth introduction?



## Informal Landscape

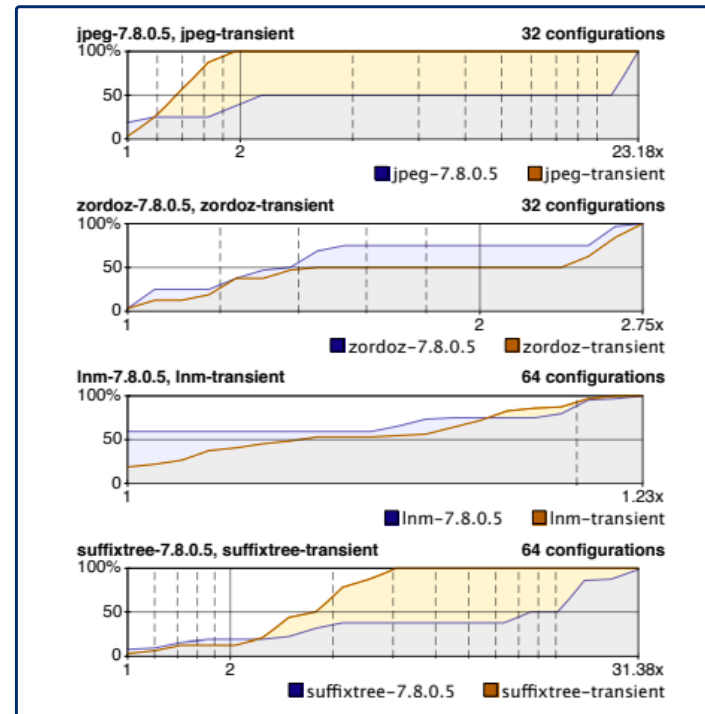
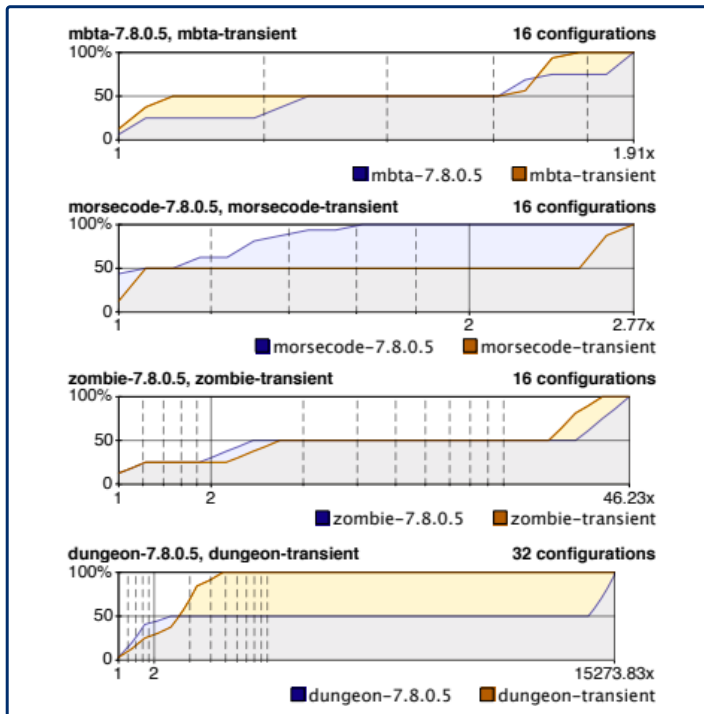


## Deep + Shallow

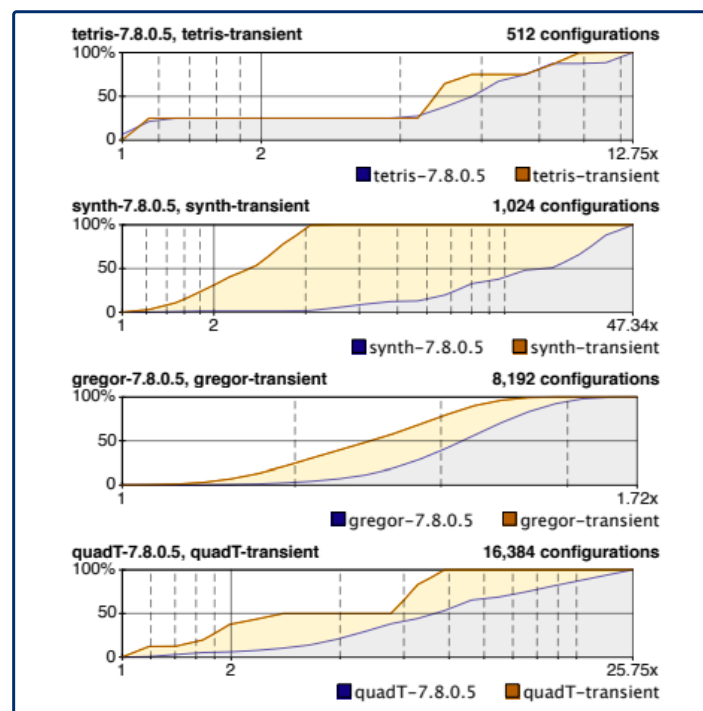
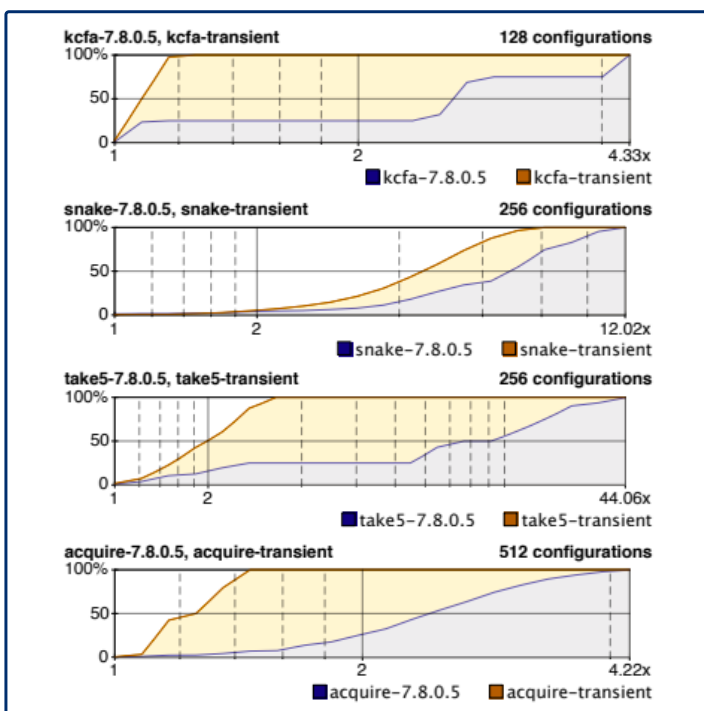
| Benchmark | Best w/ D+S | Benchmark  | Best w/ D+S |
|-----------|-------------|------------|-------------|
| forth     | 12%         | zordoz     | 47%         |
| fsm       | 38%         | lnm        | 66%         |
| fsmoo     | 31%         | suffixtree | 48%         |
| mbta      | 19%         | kcfa       | 55%         |
| morsecode | 25%         | snake      | 46%         |
| zombie    | 6%          | take5      | 36%         |
| dungeon   | 31%         | acquire    | 64%         |
| jpeg      | 38%         | tetris     | 62%         |

Percent of gradual points that run fastest with a **Deep+Shallow** mix

## Deep or Shallow (1/2)



## Deep or Shallow (2/2)



## Prior Work

|                               | <b>Guarded</b> | <b>Transient</b> | <b>Erasure</b> |
|-------------------------------|----------------|------------------|----------------|
| <b>type soundness</b>         |                |                  |                |
| <b>dyn. gradual guarantee</b> |                |                  |                |
| <b>blame theorem</b>          |                |                  |                |

## Prior Work

|                        | Guarded | Transient | Erasure |
|------------------------|---------|-----------|---------|
| type soundness         | ✓       | ✓         | ✗       |
| dyn. gradual guarantee | ✓       | ✓         | ✓       |
| blame theorem          | ✓       | ✓         | ✓       |

Standard tools **do not** tell the difference!



## A Toolbox to Measure Type Guarantees

**Guarded**      **Transient**

## A Toolbox to Measure Type Guarantees

|                     | Guarded | Transient |
|---------------------|---------|-----------|
| complete monitoring | ✓       | ✗         |

**CM:** Do types protect all channels?

## A Toolbox to Measure Type Guarantees

|                     | Guarded | Transient |
|---------------------|---------|-----------|
| complete monitoring | ✓       | ✗         |
| blame soundness     | ✓       | ✗         |
| blame completeness  | ✓       | ✗         |

**CM:** Do types protect all channels?

**BS:** Do errors point to *only* relevant channels?

**BC:** Do errors point to *all* relevant channels?

## A Toolbox to Measure Type Guarantees

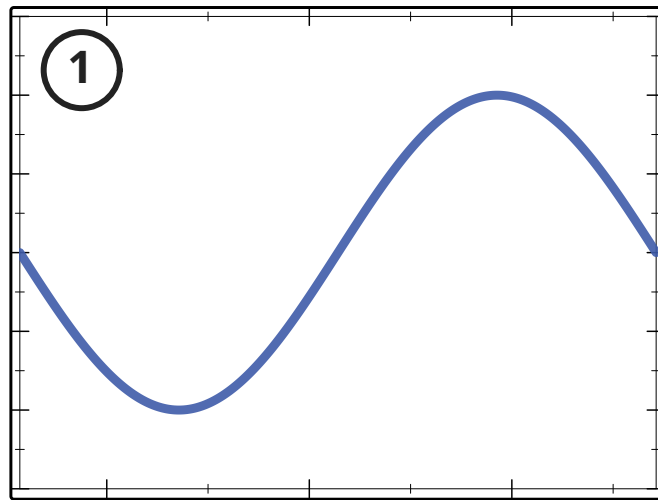
|                     | Guarded | C | F | Transient | A | E |
|---------------------|---------|---|---|-----------|---|---|
| type soundness      |         |   |   |           |   |   |
| complete monitoring |         |   |   |           |   |   |
| blame soundness     |         |   |   |           |   |   |
| blame completeness  |         |   |   |           |   |   |
| error preorder      |         |   |   |           |   |   |

## A Toolbox to Measure Type Guarantees

|                     | Guarded                             | C | F | Transient | A | E |
|---------------------|-------------------------------------|---|---|-----------|---|---|
| type soundness      | ✓                                   | ✓ | ✓ | y         | ✓ | ✗ |
| complete monitoring | ✓                                   | ✓ | ✗ | ✗         | ✗ | ✗ |
| blame soundness     | ✓                                   | ✓ | ✓ | h         | ✓ | 0 |
| blame completeness  | ✓                                   | ✓ | ✓ | ✗         | ✓ | ✗ |
| error preorder      | Guarded < C < F < Transient = A < E |   |   |           |   |   |

## Example: Clickable Plot

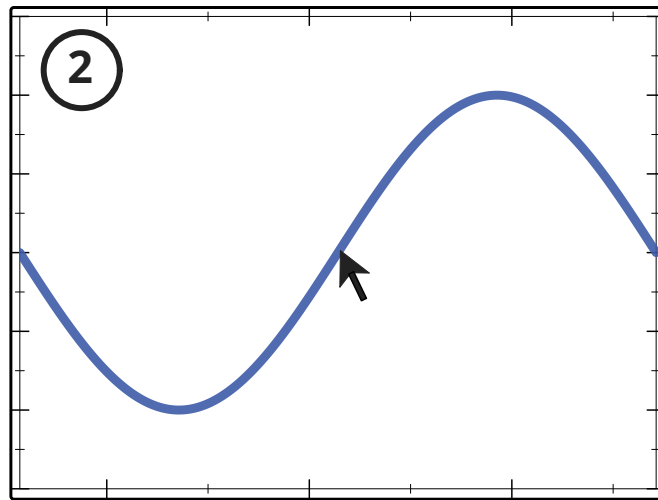
Type Soundness cannot distinguish **Guarded** and **Transient**



1. Plot data
2. Listen for a click
3. Draw an image

## Example: Clickable Plot

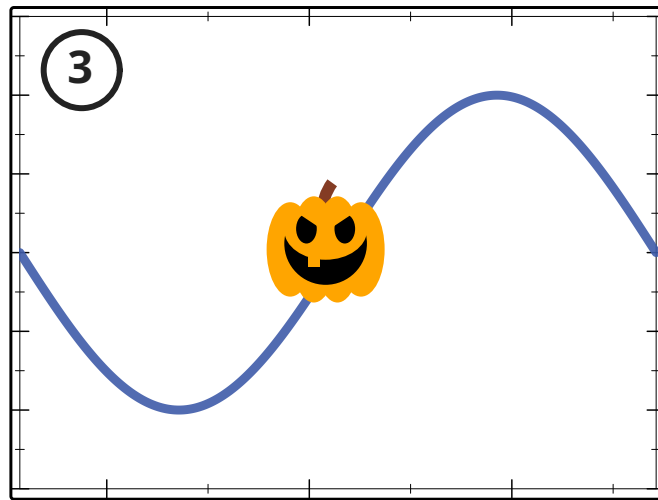
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## Example: Clickable Plot

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```
type ClickPlot
  init
    Num, Num -> Image

  mouseHandler
    MouseEvt -> Void

  show
    -> Void
```

```
class ClickPlot
  init(onClick)
    # set up

  mouseHandler(evt)
    i = onClick(evt)
    # add image

  show()
    # display
```

## Example: Clickable Plot

Type Soundness cannot distinguish **Guarded** and **Transient**

```
function h(x)
  if 0 < fst(x)
    pumpkin
  else
    fish

p = ClickPlot(h)
p.show()
# user clicks
```

```
type ClickPlot
  init
    Num, Num -> Image

  mouseHandler
    MouseEvt -> Void

  show
    -> Void
```

```
class ClickPlot
  init(onClick)
    # set up

  mouseHandler(evt)
    i = onClick(evt)
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```
function h(x)
  if 0 < fst(x)
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p = ClickPlot
p.show()
# user click
```

```
type ClickPlot
  init
  Num, Num -> Image
```

```
class ClickPlot
  init(onClick)
  # set up
  handler(evt)
  onClick(evt)
  image
  play
```

**Guarded:** error at the **type boundary**  
(coordinate pair vs. mouse event)

**Transient:** error **within** the client  
the real issue is **off the stack!**

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